UNIVERSITY OF BOLTON

OFF CAMPUS DIVISION

WESTERN INTERNATIONAL COLLEGE

BA (HONS) ACCOUNTANCY

SEMESTER ONE EXAMINATIONS 2022/2023

QUANTITATIVE METHODS FOR ACCOUNTANTS

MODULE NO: ACC4018

Date: Wednesday 11th January 2023

Time: 1:00 – 4:00

INSTRUCTIONS TO CANDIDATES:

There are FOUR compulsory questions on this paper.

Answer <u>ALL FOUR</u> questions.

All questions carry equal marks.

Calculators may be used but full workings must be shown.

Formulae books, which contain statistical tables.

Graph paper (four sheets).

Question 1

A farmer produces two products: X and Y. The farmer employs 150 skilled workers and 100 unskilled workers, and works 40 hours a week. Production of each product X takes 5 skilled hours and 2 unskilled hours. Whereas, production of product Y takes 4 skilled hours and 6 unskilled hours.

The contribution to profit that can be obtained is £15 per unit from X, and £25 per unit from Y.

a) Arrange the given information into tabular form.

(5 Marks)

b) Translate the problem into a linear programming one, identifying and writing down the objective function and the constraints.

(3 marks)

c) Use the algebraic method to calculate how many units of product X and Y would be produced to maximise profitability.

(7 marks)

d) Plot the inequalities on a graph and identify the feasible region.

(10 marks)

(Total 25 marks)

PLEASE TURN THE PAGE

Question 2

A high school boy takes part in a long jump competition. He takes three attempts at jumping and scoring the highest score.

The probabilities are as follows:

They have a 0.70 probability of successfully scoring the highest score at their first attempt.

If they succeed at the first attempt, the same probability applies on the next two attempts.

If they are not successful at any time, the probability of succeeding on any subsequent attempts is only 0.2.

Use a tree diagram to find the probabilities that:

a) Draw a tree diagram to show the probabilities of success or failure.

(5 marks)

b) She is successful on all her first three attempts.

(5 marks)

(5 marks)

(5 marks)

(5 marks)

c) She fails at the first attempt but succeeds on the next two.

- d) She is successful just once in three attempts
- e) She is still not successful after the third attempt

(Total 25 marks)

PLEASE TURN THE PAGE

Question 3

The Table below shows a sample of distances that 40 students travelled (Km)

25	51	36	60	19	58	46	30
34	27	52	33	61	30	51	43
56	39	20	54	44	48	24	25
17	64	43	50	38	38	40	50
30	38	54	37	42	36	59	33

a) Produce a grouped frequency distribution (GFD) table for this data.

(5 marks)

b) Draw a histogram of the grouped frequency distribution, and on the same graph estimate the mode of travel.

(5 marks)

c) From the GFD calculate the mean deviation.

(5 marks)

(5 marks)

- d) From the GFD calculate the mean distance travelled.
- e) Calculate the corresponding variance and standard deviation.

(5 marks)

(Total 25 marks)

PLEASE TURN THE PAGE

Question 4

A marketing team wants to determine the relationship between the cost of advertising and sales.

The monthly sales are thought to depend on the advertising.

The table below shows a record for a random sample over 10 months. Data shows:

Month	Sales (£'000)	Advertising cost (£'000)		
1	8	10		
2	12	14		
3	4	8		
4	16	18		
5	12	14		
6	20	28		
7	10	12		
8	4	8		
9	8	10		
10	12	14		

Required:

Please show all calculation workings.

a) Draw a scatter diagram of these results.

(5 Marks)

 b) Calculate the equation of the least square regression line of "y on x" and then draw this line on the scatter diagram.

(10 Marks)

c) Calculate the Pearson's correlation coefficient, r and the coefficient of determination r².

(6 Marks)

d) Use the regression equation/line to predict the likely cost of 2 months if output is 4, and 16 respectively.

(4 marks) (Total 25 marks)

END OF QUESTIONS END OF PAPER

STATISTICAL FORMULAE

FREQUENCY DISTRIBUTIONS

Required fractile from a GFD = Lower class limit of fractile class + Fractile item – cumulative frequency Fractile up to lower class limit of fractile class × class Fractile class frequency interval $\overline{\mathbf{x}} = -----$ sum of values Mean total number of items with GFD: $\bar{\mathbf{x}} = \frac{\sum (\mathbf{f} \times \mathbf{MP})}{\sum \mathbf{f}}$ MP = class Mid Point Range = Highest value – Lowest value Quartile deviation = $(Q_3 - Q_1)/2$ Mean deviation $=\frac{\sum(x-\overline{x})}{n}$ The sign of $(x-\overline{x})$ must be ignored with GFD: M.D. = $\frac{\sum (f \times (MP - \overline{x}))}{\sum f}$ Standard deviation (s) = $\frac{\sum (x - \overline{x})^2}{\sum (x - \overline{x})^2}$ If the mean is not a rounded number: s = $-\overline{x}^2$

with GFD: $s = \sqrt{\frac{\sum(f \times MP^2)}{\sum f}}$

Variance: s^2 Coefficient of variation = $\frac{s}{\overline{x}} \times 100$

Pearson's Coefficient of Skewness (Sk) =

3 (Mean – Median) Standard Deviation

CORRELATION

Regression line of "y on x": y = a + bx

where

 $\mathbf{b} = \frac{\mathbf{n} \times \sum \mathbf{x}\mathbf{y} - \sum \mathbf{x} \times \sum \mathbf{y}}{\mathbf{n} \times \sum \mathbf{x}^2 - (\sum \mathbf{x})^2} \qquad \mathbf{a} = \frac{\sum \mathbf{y} - \mathbf{b} \times \sum \mathbf{x}}{\mathbf{n}}$

 $\mathbf{n} =$ number of pairs

 $\mathbf{r} = \sqrt{\mathbf{b}_{yx} \times \mathbf{b}_{xy}}$

Cov(x,y)

 $(S_x \times S_v)$

6∑d

 $n(n^2 - 1)$

Regression line of "x on y": $\mathbf{x} = \mathbf{a} + \mathbf{by}$ $\mathbf{n} \times \sum \mathbf{yx} - \sum \mathbf{y} \times \sum \mathbf{x}$

where

$$\mathbf{b} = \frac{\mathbf{n} \times \sum \mathbf{y} \mathbf{x} - \sum \mathbf{y} \times \sum \mathbf{x}}{\mathbf{n} \times \sum \mathbf{y}^2 - (\sum \mathbf{y})^2} \qquad \mathbf{a} = \frac{\sum \mathbf{x} - \mathbf{b} \times \sum \mathbf{y}}{\mathbf{n}}$$

Pearson product-moment Coefficient of Correlation (r)

$$\mathbf{r} = \frac{\mathbf{n} \times \sum \mathbf{xy} - \sum \mathbf{x} \times \sum \mathbf{y}}{\sqrt{((\mathbf{n} \times \sum \mathbf{x}^2 - (\sum \mathbf{x})^2) (\mathbf{n} \times \sum \mathbf{y}^2 - (\sum \mathbf{y})^2))}}$$

Coefficient of determination

$$y) = \frac{\sum (x - \overline{x})(y - \overline{y})}{p}$$

Covariance: Cov(x,y) = -

where

where

d = the *difference* between the rankings of the same item in each series

 $\mathbf{r}^2 = \mathbf{b}_{\mathbf{v}\mathbf{x}} \times \mathbf{b}_{\mathbf{x}\mathbf{y}}$

PROBABILITY

Multiplication rule: the prob. of a sequential event is the product of all its elementary events $P(A \cap B \cap C \cap ...) = P(A) \times P(B) \times P(C) ...$

Addition rule: the prob. of one of a number of mutually exclusive events occurring is the sum of theprobabilities of the events $P(X \cup Y \cup Z \cup ...) = P(X) + P(Y) + P(Z) ...$

Bayes' Theorem $P(E \mid S) = \frac{P(E) \times P(S \mid E)}{\sum_{i} (P(E_i) \times P(S \mid E_i))}$

S is the subsequent event and there are n prior events, E.

PROBABILITY DISTRIBUTIONS

Binomial distribution

$$P(x) = \binom{n}{x} p^x q^{n-x}$$

 $\mathbf{P}(\mathbf{x}) = \mathbf{e}^{-a} - \frac{a}{-a}$

]

Poisson distribution

where p = constant probability of a successq = 1 - p =probability of a failure Mean = npStandard deviation = \sqrt{npq}

where $e \cong 2.718$ is a constant Mean = a = npStandard deviation = \sqrt{a}

Simplified Poisson

$$\mathbf{P}(x+1) = \mathbf{P}(x) \times \frac{u}{x+1}$$

 $z = \frac{x - \mu}{-\mu}$ Normal distribution: standardised value

where μ and σ are the mean and standard deviation of the actual distribution

ESTIMATION & CONFIDENCE INTERVALS

- \bar{x} , s, p sample mean, standard deviation, proportion/percentage 0
- 0 μ , σ , π – population mean, standard deviation, proportion/percentage
- \overline{x} is a **point estimate** of μ \Rightarrow s is a point estimate of σ p is a point estimate of π

Confidence intervals for a population percentage or proportion

$$\pi = p \pm z p(100 - p)$$
 for a percentage

 $\pi = p \pm z \underbrace{p(1-p)}_{n}$

for a proportion

When using normal tables: $\alpha = 100 - \text{confidence level}$

Estimation of population mean (μ) when σ is known

 $\mu = \overline{x} \pm z \, \sigma / \sqrt{n}$ (normal tables for z)

Estimation of population mean (μ) for large sample size and σ unknown $\mu = \overline{x} \pm z \, s / \sqrt{n}$ (normal tables for z)

Estimation of population mean (μ) for small sample size and σ unknown $\mu = \bar{x} \pm t \, s / \sqrt{n}$

(t-tables for t)

When using t-tables: v = n-1

Confidence intervals for paired (dependent) data

 $\mu_{\rm d} = \overline{x_{\rm d}} \pm t \, s_{\rm d} / \sqrt{n_{\rm d}}$

where "d" refers to the calculated differences

FINANCIAL MATHEMATICS

Simple interest
$$A_n = P\left(1 + \frac{i}{100} \times n\right)$$

Compound interest $A_m = P\left(1 + \frac{i}{100}\right)^n$
Effective APR = $\left(\left(1 + \frac{i}{100}\right)^n - 1\right) \times 100\%$
Straight line depreciation $A_s = P\left(1 - \frac{i}{100} \times n\right)$
Depreciation $A = P\left(1 - \frac{i}{100}\right)^n$

The future value of an initial investment A_0 is given by $A = A_0 \left(1 + \frac{i}{100}\right)^n$ and the

or

100

present value of an accumulated investment A_n is given by $A_0 = \frac{A_N}{\sqrt{1-N}}$

$$A\left(1+\frac{i}{100}\right)^{-n}$$

Loan account

If an annuity is purchased for a sum of A_0 at a rate of *i*% compounded each period then the periodic repayment is

$$R = \frac{iA_0}{1 - (1 + i)^{-n}}$$

and the present value of the annuity A0 (the loan) is

$$A_0 = \mathbb{R} \times \frac{(1+i)^n - 1}{i(1+i)^n}$$
 or equivalently $A_0 = \frac{\mathbb{R}[1-(1+i)^{-n}]}{i}$

Savings account

A savings plan/sinking fund invested for n periods at a nominal rate of i% compounded each period with a periodic investment of $\pounds P$ matures to \Im where

$$S = P(1+i) \times \left(\frac{1+i)^{2}-1}{i}\right)$$

Table 1 Areas under the standard normal curve											
	4	(area in body of table)									
							1				
:	z 0.0	00 0.	01 0.1	02 0.0	3 0.04	0.0	5 0.0	6 0.07	7 0.04	3 00	
0	.0 0.00	0.0	040 0.00	0.01	20 0.016	0 0.019	9 0.02	39 0.025	70 0.001	0.0	3
0.	.1 0.03	98 0.04	438 0.04	478 0.05 ⁻	17 0.055	7 0.059	6 0.063	36 0.027	5 0.031	9 0.03	59
0.	2 0.07	93 0.08	332 0.08	0.09	0.094	8 0.098	7 0.102	26 0.106	4 0.110	+ 0.07	23
0.	0.11	79 0.12	217 0.12	0.129	0.133	1 0.136	8 0.140	06 0.144	3 0.148	0 0.112	+1
0.	- 0.15	54 0.15	0.16	28 0.166	0.1700	0.173	6 0.177	2 0.180	8 0.184	4 0.187	79
0.!	5 0 19	15 . 0 10	50 0 10	05 0.00	•					2.107	
0.6	6 0.22	57 0.19	91 0.22		9 0.2054	0.208	B 0.212	3 0.215	7 0.2190	0.222	4
0.7	7 0.258	30 0.26	11 0.26	24 0.235	7 0.2389	0.242	2 0.245	4 0.248	6 0.2517	0.254	9
0.8	0.288	0.29	10 0.293	39 0.207	0.2/04 7 0.2005	0.2734	0.276	4 0.2794	0.2823	0.285	2 .
0.9	0.315	0.318	36 0.321	2 0.3230	0.2990 B 0.3264	0.3023	0.305 ⁻	1 0.3078	0.3106	0.313	3
				0.0200	0.0204	0.5288	0.331	0.3340	0.3365	0.338	9
1.0	0.341	3 0.343	0.346	0.3485	0.3508	0.3531	0.355	0.0577	0.000		
1.1	0.364	3 0.366	65 0.368	6 0.3708	0.3729	0.3749	0.3770	0.3577	0.3599	0.362	
1.2	0.384	9 0.386	9 0.388	8 0.3907	0.3925	0.3944	0.3962	0.3980	0.3810	0.383(
1.3	0.403	2 0.404	9 0.406	6 0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4015	
1.4	0.419	2 0.420	/ 0.422	2 0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4177	
1.5	0.4330	0.424	5. 0.405-	7 0 1						0,-010	
1.6	0.4452	0.434	0.435) C 447/	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441	:
1.7	0.4554	0.4564	0.4472	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545	
1.8	0.4641	0.4649	0.4656	0.4664	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633	1
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.45/8	0.4686	0.4693	0.4699	0.4706	
					0.1700	0.4/44	0.4750	0.4756	0.4761	0.4767	
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0 4802	0 4900	0.4040		
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4812	0.4817	-
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4897	0.4857	
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4067	0.4890	
a.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4916	
.5	0.4938	04040	0 4041	0.40.45						0.4000	
.6	0.4953	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952	
.7	0.4965	0.4966	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964	
.8	0.4974	0.4975	0.4976	0.4900	0 4969	0.4970	0.4971	0.4972	0.4973	0.4974	
.9	0.4981	0.4982	0.4982	0.4983	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981	
				0.4000	0.4504	0.4984	0.4985	0.4985	0.4986	0.4986	
.0	0.4987	0.4987	0.4987	0.4988	0.4988	0 4980	0 4000	0.4000		1	
1	0.4990	0.4991	0.4991	0.4991	0.4992	0.4992	0.4989	0.4989	0.4990	0.4990	
2	0.4993	0.4993	0.4994	0.4994	0.4994	0.4994	0.4994	0.4992	0.4993	0.4993	
3	0.4995	0.4995	0.4995	0.4996	0.4996	0.4996	0.4996	0.4995	0.4995	0.4995	
i	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4996	0.4997	
-							0.1007	0.453/	0.4997	0.4998	

00

Table 2	Percentage	points of the	t-distribution
---------	------------	---------------	----------------



	a/2
	M
-	**

		One-tailed			Two-tailed	
One tail α Two tails α	5% 10%	2.5% 5%	1% 2%	0.5% 1%	0.1% 0.2%	0.05% 0.1%
v = 1	6.31	4.30	12.71	31.82	63.66	636.6
2	2.92	4.30	6.96	9.92	22.33	31.60
3	2.35	3.18	4.54	5.84	10.21 .	12.92
4	2.13	2.78	3.75	4.60	7.17	8.61
5	2.02	2.57	3.36	4.03	5.89	6.87
6	1.94	2.45	3,14	3.71	5.21	5.96
7	1.89	2.36	3.00	3.50	4.79	5.41
8	1.86	2.31	2.90	3,36	4.50	5.04
9	1.83	2.26	2.82	3.25	4.30	4.78
10	1.81	2.23	2.76	3.17	<mark>4.14</mark>	4.59
12	1.78	2.18	2.68	3.05	3.93	4.32
15	1.75	2.13	2.60	2.95	3.73	4.07
20	1.72	2.09	2.53	2.85	3.55	3.85
24	1.71	2.06	2,49	2.80	3.47	3.75
30	1.70	2.04	2.46	2.75	3.39	3.65
40	1.68	2.02	<mark>2.</mark> 42	2.70	3 <mark>.31</mark>	3.55
60	1.67	2.00	2.39	2.66	3.23	3. <mark>46</mark>
<u>∞</u>	1.64	1.96	2.33	2.58 ·	` 3.09	3.29

v = degrees of freedom $\alpha =$ total percentage in tails



 $\alpha = total percentage in tails$