

**UNIVERSITY OF BOLTON**

**SCHOOL OF ENGINEERING**

**BEng (HONS) CIVIL ENGINEERING**

**SEMESTER ONE EXAMINATIONS 2021/2022**

**PROJECT AND ENVIRONMENTAL MANAGEMENT**

**MODULE NO: CIE6009**

Date: 10<sup>th</sup> January 2022

Time: 10:00hrs - 12:00hrs

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**INSTRUCTIONS TO CANDIDATES:**

This exam paper contains **TWO** sections: section 'A' and section 'B'

Section A contains **ONE** question: you **must** answer this question. It worth 40 marks.

Section B contains **THREE** questions: you should answer any **TWO** questions from these three questions. Each of these questions is worth 30 marks.

Marks for parts of questions are shown in brackets.

This examination paper carries a total of 100 marks.

All working must be shown.

**CANDIDATES REQUIRE:**

Formula Sheets (attached following questions).

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**Section A – Compulsory Question**

Q1.1 Which of the following is NOT one of the four steps in PRINCE2's view of project management?

- A. Plan
- B. Delegate
- C. Manage
- D. Control

Q1.2 Which of the following roles is responsible for the day-to-day running of a project?

- A. Project Manager
- B. Team Manager
- C. Corporate/Programme
- D. Project Board

Q1.3 Which Theme is concerned with uncertainty?

- A. Risk
- B. Change
- C. Manage by exception
- D. Quality

Q1.4 How many Project Managers should a PRINCE2 project have?

- A. One
- B. As many as necessary
- C. Up to two
- D. A Project Manager is optional in PRINCE2

Q1.5 Which of the following is NOT a characteristic of a PRINCE2 project?

- A. Brings about a change
- B. Repeatable
- C. Temporary
- D. Cross-functional

**Question 1 continued over the next page**

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**Question One** (Answer should be inserted in answer book as follows: Q1.1 A)

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**Question 1 continued...**

Q1.6 Which of the following does the PRINCE2® method not specifically control?

- A. Quality
- B. Scope
- C. Profits
- D. Benefits

Q1.7 Which of the following layers is the **final** authority within the Project (i.e. who makes the major decisions)?

- A. Project Manager
- B. Team Manager
- C. Corporate/Programme
- D. Project Board

Q1.8 Which of the following is NOT one of the four “integrated elements” of a PRINCE2® project?

- A. Principles
- B. Themes
- C. Processes
- D. Techniques

Q1.9 Who is the Project Board’s “Boss”?

- A. Project Manager
- B. Team Manager
- C. Corporate, Programme Management, or Customer
- D. Project Board

Q1.10 Which of the following Themes supports the “Focus On Products” principle?

- A. Business Case
- B. Risk
- C. Quality
- D. Organisation

**Question 1 continued over the next page**

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**Question 1 continued...**

Q1.11 Which of the following statements apply to a Stage Plan?

1. Is produced with the knowledge of earlier stages
2. Provides the basis for control by the Project Board
3. Is produced close to the time when the planned events will take place
4. Provides the basis for day-to-day control by the Project Manager

- A. 1, 2, 3
- B. 1, 2, 4
- C. 1, 3, 4
- D. 2, 3, 4

Q1.12 What theme ensures the project is desirable, viable and achievable?

- A. Organization
- B. Progress
- C. Business Case
- D. Risk

Q1.13 How does the Directing a Project activity support the Manage By Stages principle?

- A. Towards the end of the previous stage the Board create the plan for the next stage
- B. In Giving Ad Hoc direction the Board authorise the next stage
- C. In Authorising a Project the Project Board authorise all stage plans
- D. In Authorising a Stage or Exception Plan the Board authorise each stage (after the Initiation Stage)

Q1.14 Which one of the following Directing a Project activity is conducted at the end of the Starting up a Project process?

- A. Authorising a Stage or Exception Plan
- B. Giving Ad Hoc Direction
- C. Authorising Initiation
- D. Authorising a Project

**Question 1 continued over the next page**

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**Question 1 continued...**

Q1.15 Identify the missing words in the following sentence.

The purpose of the [ ? ] process is to establish solid foundations for the project, enabling the organization to understand the work that needs to be done to deliver the project's products.

- A. Initiating a Project
- B. Starting up a Project
- C. Directing a Project
- D. Managing a Stage Boundary

Q1.16 Which one of the following statements about the Change Theme is TRUE?

- A. The Change theme addresses how a project can prevent change
- B. The Change theme addresses how uncertainty is to be handled
- C. The Change theme defines the plan levels
- D. The Change theme acknowledges that change is inevitable and must be controlled if the project is to be successful

Q1.17 What product forms the 'contract' between the Project Manager and the Project Board for the project?

- A. Project Plan
- B. Project Product Description
- C. Project Initiation Documentation
- D. Project Brief

Q1.18 Which of the following are true about a PRINCE2 Project Management team?  
(Select the correct combination of those offered at the bottom of the question)

1. The Project Team is based on roles not jobs
2. You can have the job of "Senior Mechanic" and the role of "Team Manager"
3. Roles identify an individual's responsibilities within the Project Team
4. You can have the role of "Senior Mechanic" and the job of "Team Manager"

- A. 1,2,3
- B. 1,2,4
- C. 2,3,4
- D. 1,3,4

**Question 1 continued over the next page**

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**Question 1 continued...**

Q1.19 Which is a purpose of the Managing Product Delivery process?

- A. Controls the link between the Project Manager and the Team Manager(s)
- B. Tracks the progress of a stage with the help of Checkpoint Reports
- C. Provides a link between the work of the Project Manager and the Project Board
- D. Maintains a focus on the delivery of benefits throughout the stage

Q1.20 Which is a purpose of the Closing a Project process?

- A. Define the procedure for handing over products
- B. Provide a fixed point at which acceptance for the project product is confirmed
- C. Define formal requirements for the acceptance, execution and delivery of project work
- D. Confirm all project benefits have been achieved

**[Total 40 marks]**

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## **Section B – Answer Any Two Questions**

### **Question Two**

A civil engineering company decided to diversify its construction activities to improve its prospects of winning works in drainage and earthwork areas. It considers investing heavily in new equipment and machinery to meet the expected work. The board of directors considers three types of plant (A, B and C) for investment:

**Each of the three plant types** requires an initial investment of £30,000. In return, the company is expected to receive annual payments from operation of each plant as detailed in **Table Q2**. There is no scrap value for all plant at the end of the investment period and the cost of capital finance is 10%.

Appraise the three investments using the following methods:

- (i) The Payback Period (**PBP**) (7 marks)
- (ii) The Accounting Rate of Return (**ARR**) (8 marks)
- (iii) The Net Present Value (**NPV**) (8 marks)
- (iv) Explain the reasons for your advice to the company (7 marks)

[Total 30 marks]

Year	Investment Plant		
	A	B	C
0	-30,000	-30,000	-30,000
1	£5,500	£8,500	£9,000
2	£6,500	£8,500	£8,000
3	£8,500	£8,500	£9,000
4	£10,500	£8,500	£6,000
5	£10,500	£7,000	£5,500
6	£9,500	£6,000	£4,000

**Table Q2**



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**Question Three**

- (a) Using an annotated diagram, explain the process of Design and Build (D & B) method of construction procurement and mention four of its advantages and four of its disadvantages.

In your explanation, state what Design Novation means and its advantages to the client, designer and contractor.

**(10 marks)**

- (b) Evaluate the PFI contract process and discuss its main benefits and drawbacks.

**(10 marks)**

- (c) Critically discuss the challenges, which could be faced when applying value management processes in the construction industry.

**(10 marks)**

**[Total 30 marks]**

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### Question Four

A contractor is preparing to bid for a contract with one of the utilities company. The contract is expected to run for a period of year with a possibility of extension to 4, 5 or 6 years. The bid will involve an initial capital outlay of £315,000 for the purchase of specialist equipment.

A risk analysis shows that the annual profit for the contract could be £84,000, £100,000 or £116,000 with respective probabilities of 0.3, 0.5 and 0.2. It also indicates that the profit could vary with contract duration in accordance with the probabilities set out in Table Q4 below.

Project life	Annual Profit and Probabilities		
	£84,000	£100,000	£116,000
4 years	0.3	0.2	0.3
5 years	0.4	0.4	0.3
6 years	0.3	0.4	0.4

**Table Q4**

The salvage value of the specialist equipment is estimated as being £24,000, £16,000 and £10,000 after 4, 5 and 6 years respectively.

The contractor requires a minimum return of 10% on all investments.

Assemble the data necessary for the plotting of an investment risk profile and justify the conclusions you would reach based upon this data.

**[Total 30 marks]**

**END OF QUESTIONS**

**FORMULA SHEET ON FOLLOWING PAGE....**

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**Useful Formulae**

$$(1) \quad NPV = \sum_i^n CF_i \times DCF_i$$

where,

NPV = Net present value

$CF_i$  = Cashflow at year  $i$

$DCF_i$  = Discount cashflow factor for  $i$  year and interest rate,  $k$ , given as  $= \frac{1}{(1+k)^i}$

$n$  = Number of years

$$(2) \quad ARR = \frac{\text{Average Annual Profit}}{\text{Initial Investment}} \times 100$$

where,

**ARR** = Accounting Rate of Return

$\text{Average Annual Profit} = \frac{\sum_i^n CF_i - \text{Total Depreciation}}{n}$ , with  $CF_i$  defined as cashflow in year  $i$

Initial Investment = Initial capital investment put in project

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Table A-1 Future Value Interest Factors for One Pound Compounded at  $k$  Percent for  $n$  Years:  $FVIF_{k,n} = (1 + k)^n$

Year	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	20%	24%	25%	30%
1	1.0100	1.0200	1.0300	1.0400	1.0500	1.0600	1.0700	1.0800	1.0900	1.1000	1.1100	1.1200	1.1300	1.1400	1.1500	1.1600	1.2000	1.2400	1.2500	1.3000
2	1.0201	1.0404	1.0609	1.0816	1.1025	1.1236	1.1449	1.1664	1.1881	1.2100	1.2321	1.2544	1.2769	1.2996	1.3225	1.3456	1.4400	1.5376	1.5625	1.6900
3	1.0303	1.0612	1.0927	1.1249	1.1576	1.1910	1.2250	1.2597	1.2950	1.3310	1.3676	1.4049	1.4429	1.4815	1.5209	1.5609	1.7280	1.9066	1.9531	2.1970
4	1.0406	1.0824	1.1255	1.1699	1.2155	1.2625	1.3108	1.3605	1.4116	1.4641	1.5181	1.5735	1.6305	1.6890	1.7490	1.8106	2.0736	2.3642	2.4414	2.8561
5	1.0510	1.1041	1.1593	1.2167	1.2763	1.3382	1.4026	1.4693	1.5386	1.6105	1.6851	1.7623	1.8424	1.9254	2.0114	2.1003	2.4883	2.9316	3.0518	3.7129
6	1.0615	1.1262	1.1941	1.2653	1.3401	1.4185	1.5007	1.5869	1.6771	1.7716	1.8704	1.9738	2.0820	2.1950	2.3131	2.4364	2.9860	3.6352	3.8147	4.8268
7	1.0721	1.1487	1.2299	1.3159	1.4071	1.5036	1.6058	1.7138	1.8280	1.9487	2.0762	2.2107	2.3526	2.5023	2.6600	2.8262	3.5832	4.5077	4.7684	6.2749
8	1.0829	1.1717	1.2668	1.3686	1.4775	1.5938	1.7182	1.8509	1.9926	2.1436	2.3045	2.4760	2.6584	2.8526	3.0590	3.2784	4.2998	5.5895	5.9605	8.1573
9	1.0937	1.1951	1.3048	1.4233	1.5513	1.6895	1.8385	1.9990	2.1719	2.3579	2.5580	2.7731	3.0040	3.2519	3.5179	3.8030	5.1598	6.9310	7.4506	10.604
10	1.1046	1.2190	1.3439	1.4802	1.6289	1.7908	1.9672	2.1589	2.3674	2.5937	2.8394	3.1058	3.3946	3.7072	4.0456	4.4114	6.1917	8.5944	9.3132	13.786
11	1.1157	1.2434	1.3842	1.5395	1.7103	1.8983	2.1049	2.3316	2.5804	2.8531	3.1518	3.4785	3.8359	4.2262	4.6524	5.1173	7.4301	10.657	11.642	17.922
12	1.1268	1.2682	1.4258	1.6010	1.7959	2.0122	2.2522	2.5182	2.8127	3.1384	3.4985	3.8960	4.3345	4.8179	5.3503	5.9360	8.9161	13.215	14.552	23.298
13	1.1381	1.2936	1.4685	1.6651	1.8856	2.1329	2.4098	2.7196	3.0658	3.4523	3.8833	4.3635	4.8980	5.4924	6.1528	6.8858	10.699	16.386	18.190	30.288
14	1.1495	1.3195	1.5126	1.7317	1.9799	2.2609	2.5785	2.9372	3.3417	3.7975	4.3104	4.8871	5.5348	6.2613	7.0757	7.9875	12.839	20.319	22.737	39.374
15	1.1610	1.3459	1.5580	1.8009	2.0789	2.3966	2.7590	3.1722	3.6425	4.1772	4.7846	5.4736	6.2543	7.1379	8.1371	9.2655	15.407	25.196	28.422	51.186
16	1.1726	1.3728	1.6047	1.8730	2.1829	2.5404	2.9522	3.4259	3.9703	4.5950	5.3109	6.1304	7.0673	8.1372	9.3576	10.748	18.488	31.243	35.527	66.542
17	1.1843	1.4002	1.6528	1.9479	2.2920	2.6928	3.1588	3.7000	4.3276	5.0545	5.8951	6.8660	7.9861	9.2765	10.761	12.468	22.186	38.741	44.409	86.504
18	1.1961	1.4282	1.7024	2.0258	2.4066	2.8543	3.3799	3.9960	4.7171	5.5599	6.5436	7.6900	9.0243	10.575	12.375	14.463	26.623	48.039	55.511	112.455
19	1.2081	1.4568	1.7535	2.1068	2.5270	3.0256	3.6165	4.3157	5.1417	6.1159	7.2633	8.6128	10.197	12.056	14.232	16.777	31.948	59.568	69.389	146.192
20	1.2202	1.4859	1.8061	2.1911	2.6533	3.2071	3.8697	4.6610	5.6044	6.7275	8.0623	9.6463	11.523	13.743	16.367	19.461	38.338	73.864	86.736	190.050
21	1.2324	1.5157	1.8603	2.2788	2.7860	3.3996	4.1406	5.0338	6.1088	7.4002	8.9492	10.804	13.021	15.668	18.822	22.574	46.005	91.592	108.420	247.065
22	1.2447	1.5460	1.9161	2.3699	2.9253	3.6035	4.4304	5.4365	6.6586	8.1403	9.9336	12.100	14.714	17.861	21.645	26.186	55.206	113.574	135.525	321.184
23	1.2572	1.5769	1.9736	2.4647	3.0715	3.8197	4.7405	5.8715	7.2579	8.9543	11.026	13.552	16.627	20.362	24.891	30.376	66.247	140.831	169.407	417.539
24	1.2697	1.6084	2.0328	2.5633	3.2251	4.0489	5.0724	6.3412	7.9111	9.8497	12.239	15.179	18.788	23.212	28.625	35.236	79.497	174.631	211.758	542.801
25	1.2824	1.6406	2.0938	2.6658	3.3864	4.2919	5.4274	6.8485	8.6231	10.835	13.585	17.000	21.231	26.462	32.919	40.874	95.396	216.542	264.698	705.641
30	1.3478	1.8114	2.4273	3.2434	4.3219	5.7435	7.6123	10.063	13.268	17.449	22.892	29.960	39.116	50.950	66.212	85.850	237.376	634.820	807.794	*
35	1.4166	1.9999	2.8139	3.9461	5.5160	7.6861	10.677	14.785	20.414	28.102	38.575	52.800	72.069	98.100	133.176	180.314	590.668	*	*	*
36	1.4308	2.0399	2.8983	4.1039	5.7918	8.1473	11.424	15.968	22.251	30.913	42.818	59.136	81.437	111.834	153.152	209.164	708.802	*	*	*
40	1.4889	2.2080	3.2620	4.8010	7.0400	10.286	14.974	21.725	31.409	45.259	65.001	93.051	132.782	188.884	267.864	378.721	*	*	*	*
50	1.6446	2.6916	4.3839	7.1067	11.467	18.420	29.457	46.902	74.358	117.391	184.565	289.002	450.736	700.233	*	*	*	*	*	*



Table A-3 Present Value Interest Factors for One Pound Discounted at  $k$  Percent for  $n$  Years:  $PVIF_{k,n} = 1 / (1 + k)^n$

Year	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	20%	24%	25%	30%
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.9009	0.8929	0.8850	0.8772	0.8696	0.8621	0.8333	0.8065	0.8000	0.7692
2	0.9803	0.9612	0.9426	0.9246	0.9070	0.8900	0.8734	0.8573	0.8417	0.8264	0.8116	0.7972	0.7831	0.7695	0.7561	0.7432	0.6944	0.6504	0.6400	0.5917
3	0.9706	0.9423	0.9151	0.8890	0.8638	0.8396	0.8163	0.7938	0.7722	0.7513	0.7312	0.7118	0.6931	0.6750	0.6575	0.6407	0.5787	0.5245	0.5120	0.4552
4	0.9610	0.9238	0.8885	0.8548	0.8227	0.7921	0.7629	0.7350	0.7084	0.6830	0.6587	0.6355	0.6133	0.5921	0.5718	0.5523	0.4823	0.4230	0.4096	0.3501
5	0.9515	0.9057	0.8626	0.8219	0.7835	0.7473	0.7130	0.6806	0.6499	0.6209	0.5935	0.5674	0.5428	0.5194	0.4972	0.4761	0.4019	0.3411	0.3277	0.2693
6	0.9420	0.8880	0.8375	0.7903	0.7462	0.7050	0.6663	0.6302	0.5963	0.5645	0.5346	0.5066	0.4803	0.4556	0.4323	0.4104	0.3349	0.2751	0.2621	0.2072
7	0.9327	0.8706	0.8131	0.7599	0.7107	0.6651	0.6227	0.5835	0.5470	0.5132	0.4817	0.4523	0.4251	0.3996	0.3759	0.3538	0.2791	0.2218	0.2097	0.1594
8	0.9235	0.8535	0.7894	0.7307	0.6768	0.6274	0.5820	0.5403	0.5019	0.4665	0.4339	0.4039	0.3762	0.3506	0.3269	0.3050	0.2326	0.1789	0.1678	0.1226
9	0.9143	0.8368	0.7664	0.7026	0.6446	0.5919	0.5439	0.5002	0.4604	0.4241	0.3909	0.3606	0.3329	0.3075	0.2843	0.2630	0.1938	0.1443	0.1342	0.0943
10	0.9053	0.8203	0.7441	0.6756	0.6139	0.5584	0.5083	0.4632	0.4224	0.3855	0.3522	0.3220	0.2946	0.2697	0.2472	0.2267	0.1615	0.1164	0.1074	0.0725
11	0.8963	0.8043	0.7224	0.6496	0.5847	0.5268	0.4751	0.4289	0.3875	0.3505	0.3173	0.2875	0.2607	0.2366	0.2149	0.1954	0.1346	0.0938	0.0859	0.0558
12	0.8874	0.7885	0.7014	0.6246	0.5568	0.4970	0.4440	0.3971	0.3555	0.3186	0.2858	0.2567	0.2307	0.2076	0.1869	0.1685	0.1122	0.0757	0.0687	0.0429
13	0.8787	0.7730	0.6810	0.6006	0.5303	0.4688	0.4150	0.3677	0.3262	0.2897	0.2575	0.2292	0.2042	0.1821	0.1625	0.1452	0.0935	0.0610	0.0550	0.0330
14	0.8700	0.7579	0.6611	0.5775	0.5051	0.4423	0.3878	0.3405	0.2992	0.2633	0.2320	0.2046	0.1807	0.1597	0.1413	0.1252	0.0779	0.0492	0.0440	0.0254
15	0.8613	0.7430	0.6419	0.5553	0.4810	0.4173	0.3624	0.3152	0.2745	0.2394	0.2090	0.1827	0.1599	0.1401	0.1229	0.1079	0.0649	0.0397	0.0352	0.0195
16	0.8528	0.7284	0.6232	0.5339	0.4581	0.3936	0.3387	0.2919	0.2519	0.2176	0.1883	0.1631	0.1415	0.1229	0.1069	0.0930	0.0541	0.0320	0.0281	0.0150
17	0.8444	0.7142	0.6050	0.5134	0.4363	0.3714	0.3166	0.2703	0.2311	0.1978	0.1696	0.1456	0.1252	0.1078	0.0929	0.0802	0.0451	0.0258	0.0225	0.0116
18	0.8360	0.7002	0.5874	0.4936	0.4155	0.3503	0.2959	0.2502	0.2120	0.1799	0.1528	0.1300	0.1108	0.0946	0.0808	0.0691	0.0376	0.0208	0.0180	0.0089
19	0.8277	0.6864	0.5703	0.4746	0.3957	0.3305	0.2765	0.2317	0.1945	0.1635	0.1377	0.1161	0.0981	0.0829	0.0703	0.0596	0.0313	0.0168	0.0144	0.0068
20	0.8195	0.6730	0.5537	0.4564	0.3769	0.3118	0.2584	0.2145	0.1784	0.1486	0.1240	0.1037	0.0868	0.0728	0.0611	0.0514	0.0261	0.0135	0.0115	0.0053
21	0.8114	0.6598	0.5375	0.4388	0.3589	0.2942	0.2415	0.1987	0.1637	0.1351	0.1117	0.0926	0.0768	0.0638	0.0531	0.0443	0.0217	0.0109	0.0092	0.0040
22	0.8034	0.6468	0.5219	0.4220	0.3418	0.2775	0.2257	0.1839	0.1502	0.1228	0.1007	0.0826	0.0680	0.0560	0.0462	0.0382	0.0181	0.0088	0.0074	0.0031
23	0.7954	0.6342	0.5067	0.4057	0.3256	0.2618	0.2109	0.1703	0.1378	0.1117	0.0907	0.0738	0.0601	0.0491	0.0402	0.0329	0.0151	0.0071	0.0059	0.0024
24	0.7876	0.6217	0.4919	0.3901	0.3101	0.2470	0.1971	0.1577	0.1264	0.1015	0.0817	0.0659	0.0532	0.0431	0.0349	0.0284	0.0126	0.0057	0.0047	0.0018
25	0.7798	0.6095	0.4776	0.3751	0.2953	0.2330	0.1842	0.1460	0.1160	0.0923	0.0736	0.0588	0.0471	0.0378	0.0304	0.0245	0.0105	0.0046	0.0038	0.0014
30	0.7419	0.5521	0.4120	0.3083	0.2314	0.1741	0.1314	0.0994	0.0754	0.0573	0.0437	0.0334	0.0256	0.0196	0.0151	0.0116	0.0042	0.0016	0.0012	*
35	0.7059	0.5000	0.3554	0.2534	0.1813	0.1301	0.0937	0.0676	0.0490	0.0356	0.0259	0.0189	0.0139	0.0102	0.0075	0.0055	0.0017	0.0005	*	*
36	0.6989	0.4902	0.3450	0.2437	0.1727	0.1227	0.0875	0.0626	0.0449	0.0323	0.0234	0.0169	0.0123	0.0089	0.0065	0.0048	0.0014	*	*	*
40	0.6717	0.4529	0.3066	0.2083	0.1420	0.0972	0.0668	0.0460	0.0318	0.0221	0.0154	0.0107	0.0075	0.0053	0.0037	0.0026	0.0007	*	*	*
50	0.6080	0.3715	0.2281	0.1407	0.0872	0.0543	0.0339	0.0213	0.0134	0.0085	0.0054	0.0035	0.0022	0.0014	0.0009	0.0006	*	*	*	*

Table A-4 Present Value Interest Factors for a One Pound Annuity Discounted at  $k$  Percent for  $n$  Years:  $PVIFA = [1 - 1/(1 + k)^n] / k$

Year	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	20%	24%	25%	30%
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.9009	0.8929	0.8850	0.8772	0.8696	0.8621	0.8333	0.8065	0.8000	0.7692
2	1.9704	1.9416	1.9135	1.8861	1.8594	1.8334	1.8080	1.7833	1.7591	1.7355	1.7125	1.6901	1.6681	1.6467	1.6257	1.6052	1.5278	1.4568	1.4400	1.3609
3	2.9410	2.8839	2.8286	2.7751	2.7232	2.6730	2.6243	2.5771	2.5313	2.4869	2.4437	2.4018	2.3612	2.3216	2.2832	2.2459	2.1065	1.9813	1.9520	1.8161
4	3.9020	3.8077	3.7171	3.6299	3.5460	3.4651	3.3872	3.3121	3.2397	3.1699	3.1024	3.0373	2.9745	2.9137	2.8550	2.7982	2.5887	2.4043	2.3616	2.1662
5	4.8534	4.7135	4.5797	4.4518	4.3295	4.2124	4.1002	3.9927	3.8897	3.7908	3.6959	3.6048	3.5172	3.4331	3.3522	3.2743	2.9906	2.7454	2.6893	2.4356
6	5.7955	5.6014	5.4172	5.2421	5.0757	4.9173	4.7665	4.6229	4.4859	4.3553	4.2305	4.1114	3.9975	3.8887	3.7845	3.6847	3.3255	3.0205	2.9514	2.6427
7	6.7282	6.4720	6.2303	6.0021	5.7864	5.5824	5.3893	5.2064	5.0330	4.8684	4.7122	4.5638	4.4226	4.2883	4.1604	4.0386	3.6046	3.2423	3.1611	2.8021
8	7.6517	7.3255	7.0197	6.7327	6.4632	6.2098	5.9713	5.7466	5.5348	5.3349	5.1461	4.9676	4.7988	4.6389	4.4873	4.3436	3.8372	3.4212	3.3289	2.9247
9	8.5660	8.1622	7.7861	7.4353	7.1078	6.8017	6.5152	6.2469	5.9952	5.7590	5.5370	5.3282	5.1317	4.9464	4.7716	4.6065	4.0310	3.5655	3.4631	3.0190
10	9.4713	8.9826	8.5302	8.1109	7.7217	7.3601	7.0236	6.7101	6.4177	6.1446	5.8892	5.6502	5.4262	5.2161	5.0188	4.8332	4.1925	3.6819	3.5705	3.0915
11	10.368	9.7868	9.2526	8.7605	8.3064	7.8869	7.4987	7.1390	6.8052	6.4951	6.2065	5.9377	5.6869	5.4527	5.2337	5.0286	4.3271	3.7757	3.6564	3.1473
12	11.255	10.575	9.9540	9.3851	8.8633	8.3838	7.9427	7.5361	7.1607	6.8137	6.4924	6.1944	5.9176	5.6603	5.4206	5.1971	4.4392	3.8514	3.7251	3.1903
13	12.134	11.348	10.635	9.9856	9.3936	8.8527	8.3577	7.9038	7.4869	7.1034	6.7499	6.4235	6.1218	5.8424	5.5831	5.3423	4.5327	3.9124	3.7801	3.2233
14	13.004	12.106	11.296	10.563	9.8986	9.2950	8.7455	8.2442	7.7862	7.3667	6.9819	6.6282	6.3025	6.0021	5.7245	5.4675	4.6106	3.9616	3.8241	3.2487
15	13.865	12.849	11.938	11.118	10.380	9.7122	9.1079	8.5595	8.0607	7.6061	7.1909	6.8109	6.4624	6.1422	5.8474	5.5755	4.6755	4.0013	3.8593	3.2682
16	14.718	13.578	12.561	11.652	10.838	10.106	9.4466	8.8514	8.3126	7.8237	7.3792	6.9740	6.6039	6.2651	5.9542	5.6685	4.7296	4.0333	3.8874	3.2832
17	15.562	14.292	13.166	12.166	11.274	10.477	9.7632	9.1216	8.5436	8.0216	7.5488	7.1196	6.7291	6.3729	6.0472	5.7487	4.7746	4.0591	3.9099	3.2948
18	16.398	14.992	13.754	12.659	11.690	10.828	10.059	9.3719	8.7556	8.2014	7.7016	7.2497	6.8399	6.4674	6.1280	5.8178	4.8122	4.0799	3.9279	3.3037
19	17.226	15.678	14.324	13.134	12.085	11.158	10.336	9.6036	8.9501	8.3649	7.8393	7.3658	6.9380	6.5504	6.1982	5.8775	4.8435	4.0967	3.9424	3.3105
20	18.046	16.351	14.877	13.590	12.462	11.470	10.594	9.8181	9.1285	8.5136	7.9633	7.4694	7.0248	6.6231	6.2593	5.9288	4.8696	4.1103	3.9539	3.3158
21	18.857	17.011	15.415	14.029	12.821	11.764	10.836	10.017	9.2922	8.6487	8.0751	7.5620	7.1016	6.6870	6.3125	5.9731	4.8913	4.1212	3.9631	3.3198
22	19.660	17.658	15.937	14.451	13.163	12.042	11.061	10.201	9.4424	8.7715	8.1757	7.6446	7.1695	6.7429	6.3587	6.0113	4.9094	4.1300	3.9705	3.3230
23	20.456	18.292	16.444	14.857	13.489	12.303	11.272	10.371	9.5802	8.8832	8.2664	7.7184	7.2297	6.7921	6.3988	6.0442	4.9245	4.1371	3.9764	3.3254
24	21.243	18.914	16.936	15.247	13.799	12.550	11.469	10.529	9.7066	8.9847	8.3481	7.7843	7.2829	6.8351	6.4338	6.0726	4.9371	4.1428	3.9811	3.3272
25	22.023	19.523	17.413	15.622	14.094	12.783	11.654	10.675	9.8226	9.0770	8.4217	7.8431	7.3300	6.8729	6.4641	6.0971	4.9476	4.1474	3.9849	3.3286
30	25.808	22.396	19.600	17.292	15.372	13.765	12.409	11.258	10.274	9.4269	8.6938	8.0552	7.4957	7.0027	6.5660	6.1772	4.9789	4.1601	3.9950	3.3321
35	29.409	24.999	21.487	18.665	16.374	14.498	12.948	11.655	10.567	9.6442	8.8552	8.1755	7.5856	7.0700	6.6166	6.2153	4.9915	4.1644	3.9984	3.3330
36	30.108	25.489	21.832	18.908	16.547	14.621	13.035	11.717	10.612	9.6765	8.8786	8.1924	7.5979	7.0790	6.6231	6.2201	4.9929	4.1649	3.9987	3.3331
40	32.835	27.355	23.115	19.793	17.159	15.046	13.332	11.925	10.757	9.7791	8.9511	8.2438	7.6344	7.1050	6.6418	6.2335	4.9966	4.1659	3.9995	3.3332
50	39.196	31.424	25.730	21.482	18.256	15.762	13.801	12.233	10.962	9.9148	9.0417	8.3045	7.6752	7.1327	6.6605	6.2463	4.9995	4.1666	3.9999	3.3333

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