

**UNIVERSITY OF BOLTON**

**OFF CAMPUS DIVISION**

**WESTERN INTERNATIONAL COLLEGE**

**BENG(HONS) MECHANICAL ENGINEERING**

**TRIMESTER ONE EXAMINATION 2021/2022**

**ENGINEERING PRINCIPLES 1**

**MODULE NO: AME4062**

Date: Saturday 8<sup>th</sup> January 2022

Time: 10:00 – 12:00

---

**INSTRUCTIONS TO CANDIDATES:**

There are SIX questions.

Answer TWO Questions from Part A  
and TWO Questions from Part B.

All questions carry equal marks.

Marks for parts of questions are shown  
in brackets.

Electronic calculators may be used  
provided the data and program storage  
memory is cleaned prior to the  
examination.

**CANDIDATES REQUIRE:**

Formula Sheet (attached)

---

Off Campus Division  
 Western International College  
 BEng(Hons) Mechanical Engineering  
 Semester 1 Examination 2021/2022  
 Engineering Principles I  
 Module No. AME4062

**PART A**

**Q1**

- a) In a system of forces, the relationship between two forces in Newton  $F_1$  and  $F_2$  is given by:

$$F_1 + 2F_2 + 4 = 0$$

$$5F_1 + 3F_2 - 1 = 0$$

Use '**Matrices Method**' to solve for  $F_1$  and  $F_2$

**(10 marks)**

- b) Two alternating voltages are given by

$$V_1 = 10 \sin \omega t \text{ volts}$$

$$V_2 = 14 \sin \left( \omega t + \frac{\pi}{3} \right) \text{ volts}$$

Determine a sinusoidal expression for the resultant  $\mathbf{V}_R = \mathbf{V}_1 + \mathbf{V}_2$ , using sine and cosine rule and compare the results graphically.

**(10 marks)**

- c) If,  $z = 7 \left( \cos \frac{\pi}{4} + j \sin \frac{\pi}{4} \right)$ , using **De Moivre's** theorem find  $z^5$

**(5 marks)**

**Total 25 marks**

**PLEASE TURN THE PAGE.....**

Off Campus Division  
Western International College  
BEng(Hons) Mechanical Engineering  
Semester 1 Examination 2021/2022  
Engineering Principles I  
Module No. AME4062

**Q2.**

a) Use partial Fractions to expand:

$$Y(s) = \frac{x^2 + 7x + 3}{x^2(x + 3)}$$

**(10 marks)**

b) The value of a lathe originally valued at AED 30000 depreciates 15% per annum.

i) Calculate its value after 4 years.

**(5 marks)**

ii) If the machine is sold when its value is less than AED 5400. After how many years is the lathe sold?

**(5 marks)**

c) Solve the logarithmic equation

$$\log x^4 - \log x^3 = \log 5x - \log 2x$$

**(5 marks)**

**Total 25 marks**

**PLEASE TURN THE PAGE.....**

Off Campus Division  
Western International College  
BEng(Hons) Mechanical Engineering  
Semester 1 Examination 2021/2022  
Engineering Principles I  
Module No. AME4062

**Q3.**

a) The law connecting friction  $F$  and load  $L$  for an experiment is given by

$$F = aL - Mb,$$

where  $a$ ,  $b$  &  $M$  are constants. Given that when  $F=6.84\text{N}$ .,  $L= 2.3\text{N}$  ,  $M= 4.4$  and when  $F= 1.23\text{N}$ ,  $L=8.5\text{N}$ ,  $M = 6.7$ . Find the following:

i) the value of  $a$  &  $b$  using **determinant method** (8 marks)

ii) find the value of  $F$  when  $L = 6.0$  and  $M = 0$  (2 marks)

b) Use partial fractions to expand

$$\frac{5x^2 - 17x + 15}{(x - 1)(x - 2)^2}$$

(10 marks)

c) Solve, correct to 4 significant figures:

$$e^{(x+1)} = 3e^{(2x-5)}$$

(5 marks)

**Total 25 marks**

**END OF PART A**

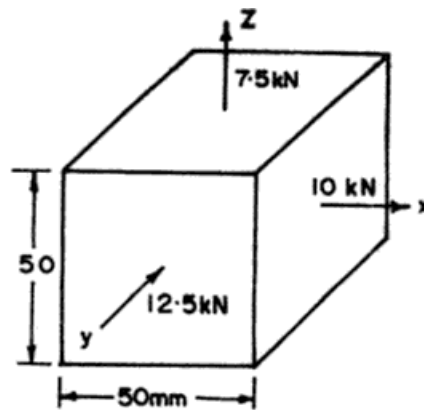
**PLEASE TURN THE PAGE.....**

Off Campus Division  
 Western International College  
 BEng(Hons) Mechanical Engineering  
 Semester 1 Examination 2021/2022  
 Engineering Principles I  
 Module No. AME4062

**PART B**

**Q4.**

A steel cube block of 50mm side is subjected to a force of 10kN (tension), 12.5kN (compression) and 7.5kN (tension) along x, y and z directions respectively as shown in **Figure Q4**.



**Figure Q4.** Steel cube block

Determine the following:

- Stresses in x,y and z directions  
**(6 marks)**
- Assuming Poisson's ratio as 0.3, find in terms of modulus of elasticity of the material E, the strains in the direction of each force.  
**(6 marks)**
- If modulus of elasticity  $E=200\text{kN/mm}^2$ , find the values of the modulus of rigidity and bulk modulus for the material of the block.  
**(8marks)**
- The change in volume of the block due to loading specified above.  
**(5 marks)**

**Total 25 marks**  
**PLEASE TURN THE PAGE.....**

Off Campus Division  
Western International College  
BEng(Hons) Mechanical Engineering  
Semester 1 Examination 2021/2022  
Engineering Principles I  
Module No. AME4062

**Q5.**

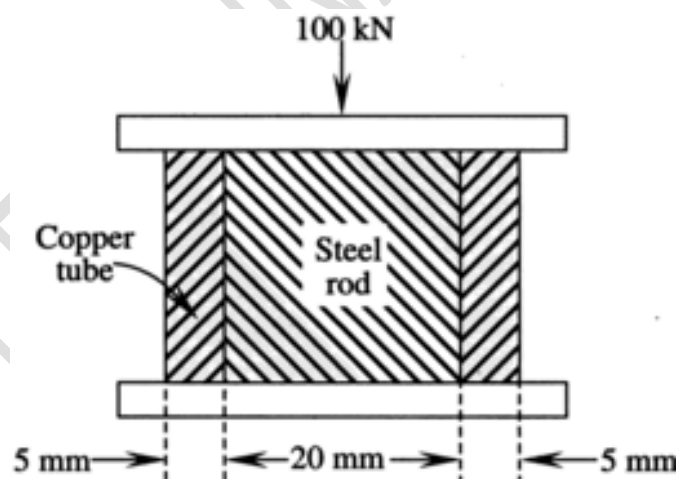
a) A compound bar consists of a circular rod of steel of diameter 20mm rigidly fitted into a copper tube of internal diameter 20mm and thickness 5mm as shown in Figure Q5a. If the bar is subjected to a load of 100kN, determine the following:

i. Stress developed in steel rod  
(5 marks)

ii. Stress developed in copper tube  
(5 marks)

Take modulus of elasticity,  $E$  of steel as 200GPa and  $E$  of copper as 120GPa

iii. Define compound bar and its rules of calculation  
(5 marks)



**Figure Q5a.** A Compound bar

**Q5 continued over the page...**

**PLEASE TURN THE PAGE.....**

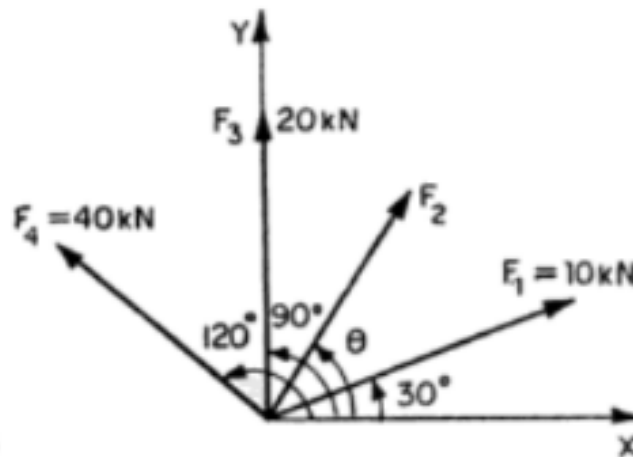
Off Campus Division  
 Western International College  
 BEng(Hons) Mechanical Engineering  
 Semester 1 Examination 2021/2022  
 Engineering Principles I  
 Module No. AME4062

**Q5 continued...**

- b) The resultant of four concurrent forces which are acting at a point O as shown in figure Q5b is along Y-axis. The magnitude of forces  $F_1$ ,  $F_3$  and  $F_4$  are 10kN, 20kN and 40kN respectively. The angles made by 10kN, 20kN and 40kN with X-axis are  $30^\circ$ ,  $90^\circ$  and  $120^\circ$  respectively.

Determine the magnitude and direction of  $F_2$  if the resultant is 72kN.

**(10 marks)**



**Figure Q5b.** Concurrent force system

**Total 25 marks**

**PLEASE TURN THE PAGE.....**

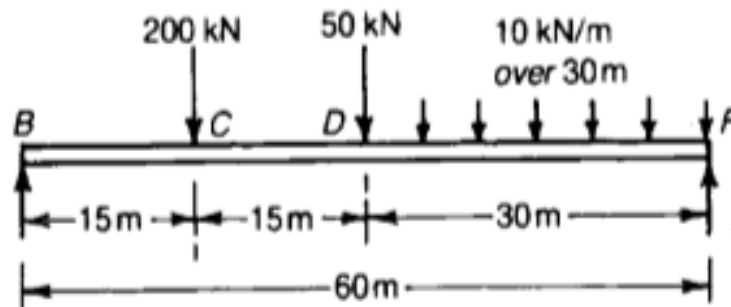
-

Off Campus Division  
Western International College  
BEng(Hons) Mechanical Engineering  
Semester 1 Examination 2021/2022  
Engineering Principles I  
Module No. AME4062

**Q6.**

A simply supported beam carries concentrated lateral loads at C and D, and a uniformly distributed lateral load over the length DF as shown in Figure Q6. Determine:

- i. Reaction loads at the support (5 marks)
- ii. Construct the shear force diagram for the beam (8 marks)
- iii. Construct the bending moment diagram for the beam (8 marks)
- iv. Find the position of maximum bending moment. (4 marks)



**Figure Q6.** Simply supported beam

**Total 25 marks**

**END OF PART B**

**END OF QUESTIONS**

**PLEASE TURN THE PAGE FOR FORMULA SHEETS...**



Off Campus Division  
 Western International College  
 BEng(Hons) Mechanical Engineering  
 Semester 1 Examination 2021/2022  
 Engineering Principles I  
 Module No. AME4062

### **FORMULA SHEET**

#### Determinants

$$\frac{x}{D_x} = \frac{-y}{D_y} = \frac{z}{D_z} = \frac{-1}{D}$$

#### Matrices

$$A^{-1} = \frac{adjA}{D}$$

$$X = A^{-1}B$$

#### Series

$$U_n = a + (n - 1) d$$

$$S_n = \frac{n}{2} [2a + (n - 1) d]$$

$$U_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_\infty = \frac{a}{1-r}$$

$$U_n = a + (n - 1)d + \frac{1}{2} (n - 1)(n - 2)C$$

#### Binomial

$$(1 + x)^n = 1 + nx + \frac{n(n-1)}{2!} x^2 + \dots$$

Validity  $|x| < 1$  Partial Fractions

$$\frac{F(x)}{(x+a)(x+b)} = \frac{A}{(x+a)} + \frac{B}{(x+b)}$$

**PLEASE TURN THE PAGE.....**

Off Campus Division  
 Western International College  
 BEng(Hons) Mechanical Engineering  
 Semester 1 Examination 2021/2022  
 Engineering Principles I  
 Module No. AME4062

$$\frac{F(x)}{(x+a)(x+b)(x+c)} = \frac{A}{(x+a)} + \frac{B}{(x+b)} + \frac{C}{(x+c)}$$

### Stress

Normal  $\sigma = \frac{P}{A}$      $A = x$ -sectional area

Shear             $\tau = \frac{P}{A}$              $A =$  shear area

### Strain

Normal             $\varepsilon = \frac{\delta l}{l}$

Shear             $\gamma = \frac{x}{y}$  (Angular Displacement in rads in direction of F)

### Compound Bars

$$P = P_1 + P_2$$

$$P = \sigma_1 A_1 + \sigma_2 A_2$$

$$\frac{\sigma_1}{E_1} = \frac{\sigma_2}{E_2}$$

### Elastic Constants

$$E = \frac{\sigma}{\varepsilon}, \quad G = \frac{\tau}{\gamma}$$

PLEASE TURN THE PAGE.....

Off Campus Division  
 Western International College  
 BEng(Hons) Mechanical Engineering  
 Semester 1 Examination 2021/2022  
 Engineering Principles I  
 Module No. AME4062

$$\varepsilon_x = \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E} - \nu \frac{\sigma_z}{E}$$

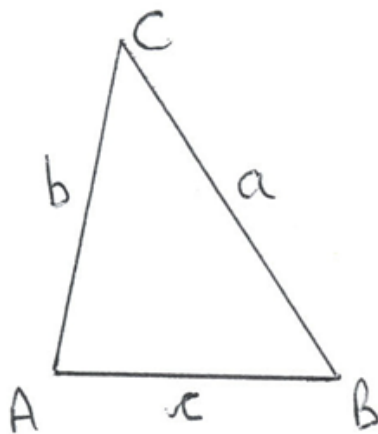
$$\varepsilon_y = \frac{\sigma_y}{E} - \nu \frac{\sigma_x}{E} - \nu \frac{\sigma_z}{E}$$

$$\varepsilon_z = \frac{\sigma_z}{E} - \nu \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E}$$

$$\varepsilon_v = \varepsilon_x + \varepsilon_y + \varepsilon_z$$

$$\varepsilon_v = \frac{1-2\nu}{E} (\sigma_x + \sigma_y + \sigma_z)$$

$$\varepsilon_v = \frac{\delta V}{V}$$



#### Compressibility

$$K = \frac{\sigma}{\varepsilon_v}$$

$$\varepsilon_v = \frac{3\sigma(1-2\nu)}{E}$$

$$E = 3K(1-2\nu)$$

$$E = 2G(1+\nu)$$

$$e_v = \frac{\delta L}{L} (1-2\mu)$$

#### Trigonometry

Sine Rule:  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine Rule:  $a^2 = b^2 + c^2 - 2bc \cos A$

**END OF FORMULA SHEET**

**END OF PAPER**