

**UNIVERSITY OF BOLTON**  
**NATIONAL CENTRE FOR MOTORSPORT**  
**ENGINEERING**  
**B.SC. (HONS) MOTORSPORT TECHNOLOGY**  
**SEMESTER TWO EXAMINATION 2018/2019**  
**ENGINEERING PRINCIPLES**  
**MODULE NUMBER MSP4011**

Date: Tuesday 21<sup>st</sup> May 2019

Time: 14:00 – 16:00

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**INSTRUCTIONS TO CANDIDATES:**

This paper has SEVEN questions  
The marks for each question are shown in  
brackets

Attempt FOUR questions

Electronic calculators may be used provided  
that data and program storage memory is  
cleared prior to the examination

Mobile telephones or cellular telephones  
may-not be used as calculators

Formula sheet attached

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**Question 1**

- (a) During a race, a driver enters and leaves the pits at 22.2m/s and is moving, entering and leaving, at this speed for 12 seconds. The car is stationary for an additional 3.2 seconds.

The average speed of the car on the track is 80 m/s. The pit lane is the same length as the circuit outside the pit lane. Ignore effects due to accelerations.

Draw a diagram to illustrate the times and speeds travelled by a pitting car and a car on the circuit with a representation of the distances involved. **(3 marks)**

Calculate the distance lost by the car during the stop. What is the loss in race time?. **(6 marks)**

- (b) During a straight-line test, a Formula Student car accelerates from zero velocity and travels 24.2 metres in 2.2 seconds. The car then travels 50.8 metres in 1.9 seconds. The car travels a total distance of 75 metres.

(i) Calculate a speed and an acceleration over the first 24.2 metres in 2.2 seconds. The car was stationary at the start. **(5 marks)**

(ii) Calculate a value for the acceleration from 24.2 metres to 75 metres in a time of 1.9 seconds. Calculate a value for the speed at 75 metres. Take the initial velocity from part (i). **(5 marks)**

- (c) A brake test machine is to simulate braking a car with a flywheel slowing from 82 radians/second to a stop in 3.5 seconds.

What is the angular acceleration of the flywheel? How many revolutions does the flywheel travel through during the braking? **(6 marks)**

The 'suvat' equations are included in the formula sheet on the last page

**Total marks 25**

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**Question 2**

**(a)** Figure Q2.1 illustrates a section on the carbon fibre tub of figure Q2.2. Compare the weight and stiffness, using areas and second moments of area, of the section of figure Q2.1 with a solid section having the same outer dimensions.

Draw diagrams of the outside of the section and the cut-out from the section. **(5 marks)**

Calculate the areas and second moment of areas of the solid section and the 'cut-out'. Hence, calculate the area and second moment of area for the section. **(8 marks)**

Compare the values with the area and second moment of area for a solid section with the same outside dimensions. Comment on the significance in terms of weight and stiffness. **(8 marks)**

**(b)** Explain the terms stiffness and strength. Using the appropriate equations explain how the shape of a component influences the stiffness and the strength of the component. **(4 marks)**

The second moment of area of a solid section is  $I = \frac{BD^3}{12}$

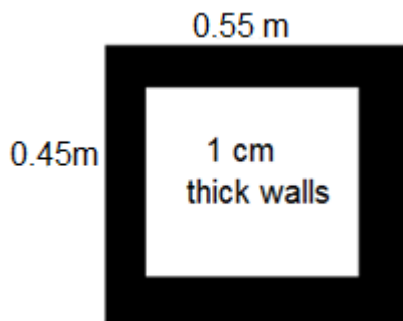


Figure Q2.1



Figure Q2.2

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**Question 3**

(a) In figure Q3a the values of  $R_1$  and  $R_2$  are  $50\Omega$  and  $150\Omega$ . What is the current through  $R_1$  and  $R_2$ ? Calculate the value of the voltage at A. What is the power required at the power supply? **(6 marks)**

(b) In the Wheatstone bridge circuit of figure Q3b the resistance  $R_1=121\Omega$  and the resistances of  $R_2$ ,  $R_3$  and  $R_4$  are each  $120\Omega$ . The applied emf,  $E=6$  volts. What is the potential difference,  $(V_a-V_b)$ ? **(6 marks)**

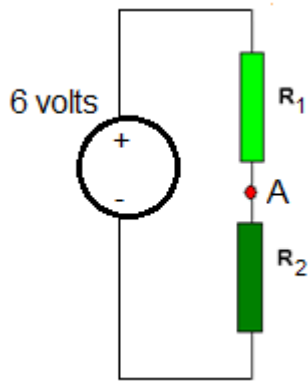


Figure Q3a

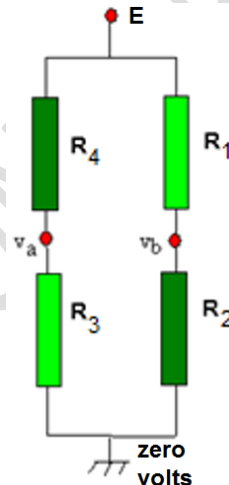


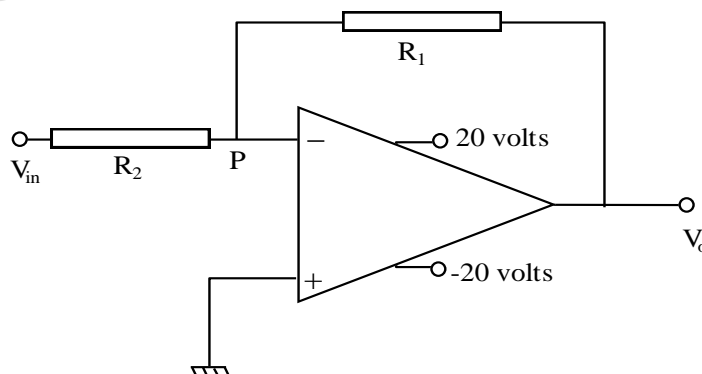
Figure Q3b

(c) Figure Q3c illustrates an inverting operational amplifier circuit. The resistors have values  $R_1=5.6k\Omega$  and  $R_2=1k\Omega$  respectively.

(i) What is the gain of the amplifier? **(2 marks)**

(ii) Annotate figure Q3c with the voltages and currents for the case where  $V_{in}=1.5$  volts. Figure Q3c is re-printed on the next page of the examination paper. **(6 marks)**

(iii) What is the operating range at the input voltage to avoid saturation at the output? Comment on the operating range in practice. **(5 marks)**



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Figure Q3c

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Figure Q3c for annotation over the page....

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For use with Question 3 Part c  
Mark on the voltages and currents

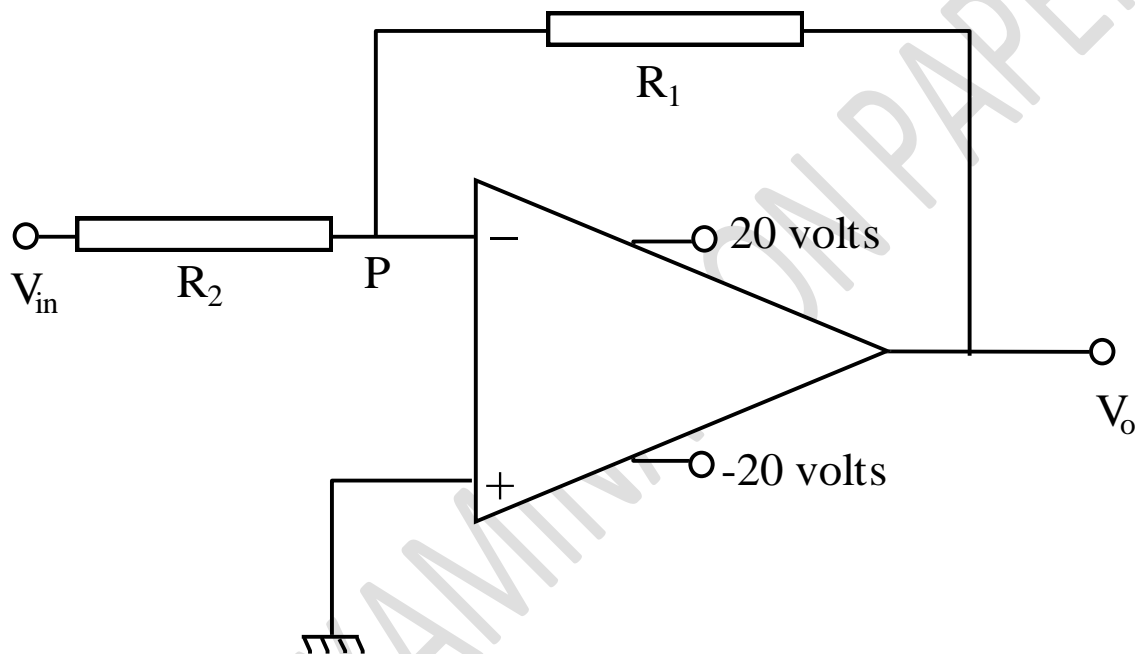


Figure Q3c ~ Circuit diagram for annotation

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#### Question 4

Figure Q4 represents part of a suspension system for a single seater race car. The pivot is fixed to the race car chassis between the upright and the spring-damper. The spring stiffness is 45kN/m.

- (i) The wheel is moved through a displacement of 25mm. Draw a diagram of the rocker clearly showing the deflection at the wheel and the corresponding deflection at the spring. Use the diagram to estimate the deflection at the spring. **(5 marks)**
- (ii) Calculate a value for the lever ratio and hence confirm the result for the deflection at the spring. **(2 marks)**
- (iii) What is the force to compress the spring at the spring? What is the force at the wheel to produce the compression at the spring? **(5 marks)**
- (iv) What is the effective stiffness of the spring at the wheel? **(5 marks)**
- (v) Explain the relationship between the lever ratio, the stiffness of the spring and the effective stiffness of the spring at the wheel. Hence, confirm the installed stiffness calculated above. **(8 marks)**

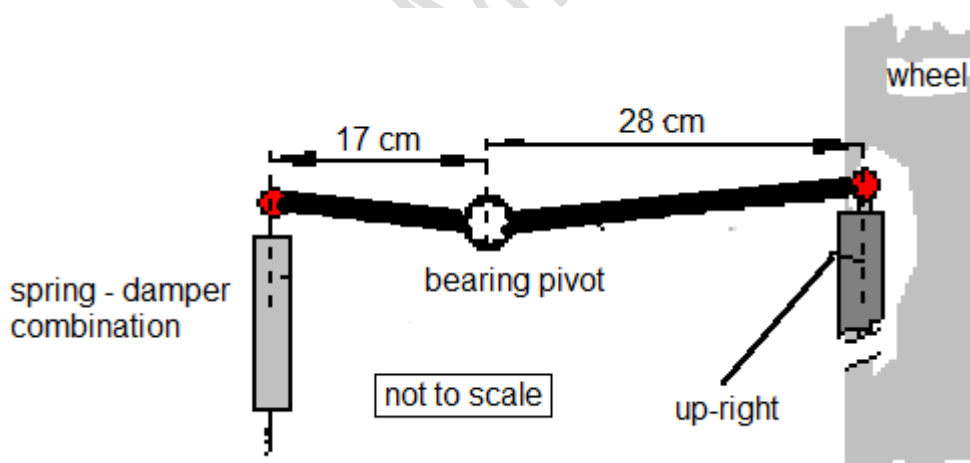


Figure Q4

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### Question 5

Figure Q5a illustrates a four-point bending test. Figure Q5b illustrates the cross section of the carbon fibre beam in Figure Q5a.

- Draw the shear force and bending moment diagrams for the beam. **(6 marks)**
- Comment on the significance of the bending moment between the supports Q and R and the significance of the positioning of a strain gauge to indicate the bending strain. **(4 marks)**
- Calculate the maximum bending stress for the loading of figure Q5a. **(8 marks)**
- Calculate a value for the Young's modulus for the beam given that the strain on the upper surface was indicated as  $503 \times 10^{-6}$  **(7 marks)**

**Total marks 25**

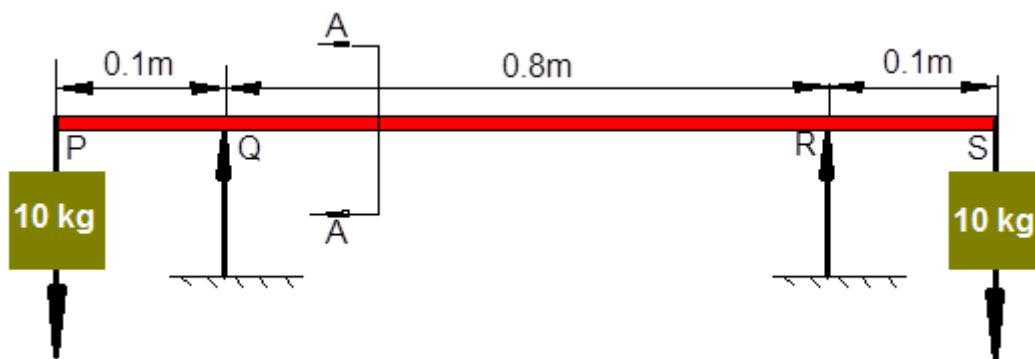
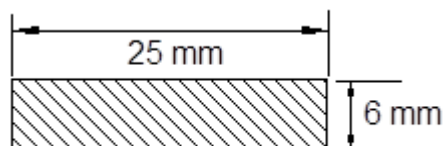


Figure Q5a



section on A-A

Figure Q5b

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**Question 6**

(a) Using appropriate diagrams explain the terms in the equations Q6a and Q6b.

**(10 marks)**

$$\frac{T}{J} = \frac{\tau}{r} = \frac{G\theta}{L} \quad \dots\text{equation (Q6a)}$$

$$J = \frac{\pi d^4}{32} \quad \dots\text{equation (Q6b)}$$

(b) A solid half shaft has a length of 0.45 metres and diameter of 25mm. The maximum load on the half shaft in a test is 750Nm. Calculate the maximum shear stress on the half shaft and the resulting twist in degrees. Take  $G=80\text{GPa}$ .

**(15 marks)**

**Total marks 25**

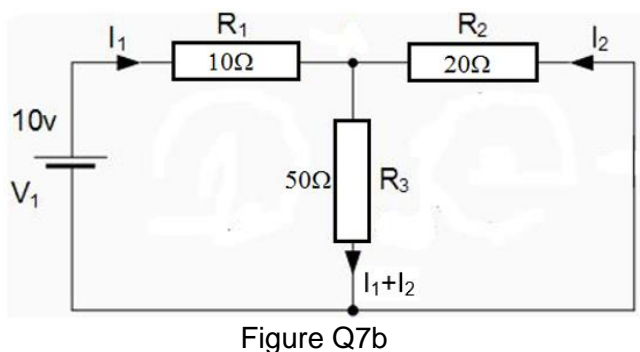
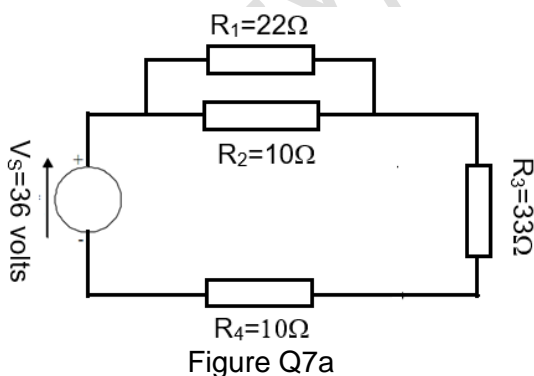
**Question 7**

(a) For the circuit of figure Q7a, determine: -

- (i) The overall resistance across  $V_s$  **(4 marks)**
- (ii) The current supplied by the voltage source  $V_s$  **(2 marks)**
- (iii) The voltage drops across each of the resistors with a check calculation **(4 marks)**
- (iv) The energy supplied by  $V_s$  in 30 minutes in joules and Wh **(4 marks)**

(b) Use Kirchoff's method of loops to find the currents,  $I_1$  and  $I_2$  in the circuit of figure Q7b. **(8 marks)**

Check your results using separate calculations **(3 marks)**



**Total marks 25**

**END OF QUESTIONS**

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### FORMULA SHEET

*Newton's Second Law:  $F = ma$  &  $T = I \alpha$  where a general expression for  $I = mk^2$*

Law of Friction:  $F = \mu R$

Torque & Power Expressions  $T = Fd$ ;  $P = Fv$

### **Kinematic Equations**

Linear Motion

$$\begin{aligned} v &= u + at \\ s &= \frac{1}{2}(u + v)t \\ s &= ut + \frac{1}{2}at^2 \\ s &= vt - \frac{1}{2}at^2 \\ v^2 &= u^2 + 2as \end{aligned}$$

Angular Motion

$$\begin{aligned} \omega_f &= \omega_i + \alpha t \\ \theta &= \frac{1}{2}(\omega_i + \omega_f)t \\ \theta &= \omega_i t + \frac{1}{2}\alpha t^2 \\ \theta &= \omega_f t - \frac{1}{2}\alpha t^2 \\ \omega_f^2 &= \omega_i^2 + 2\alpha\theta \end{aligned}$$

Linear to Angular

$$\begin{aligned} s &= r\theta \\ v &= r\omega \\ a &= r\alpha \\ \omega &= \frac{\theta}{t} \end{aligned}$$

$$\text{Centripetal Acceleration} = \frac{v^2}{R} \text{ \& } \omega^2 R$$

Ohm's Law  
 $V=IR$



Power supplied by a  
voltage source  
 $P=VI$

Power dissipated  
by a resistor  
 $P=I^2R$

Resistance of a wire

$$R = \frac{\rho L}{A}$$

Resistors in series

$$R_T = R_1 + R_2 + R_3 + \dots$$

Resistors in parallel

$$\frac{1}{R_e} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \text{etc}$$

Ohm's law  $V=IR$

Power & Energy  
 $P=VI$  &  $E=VIt$

Kirchhoff's Laws  
 $\sum I = 0$  &  $\sum \text{emf} = 0$

### **Stress equations**

Direct

$$\begin{aligned} \sigma &= \frac{F}{A} \text{ \& } E = \frac{\sigma}{\epsilon} \text{ \& } \epsilon = \frac{\delta L}{L} \\ A &= \frac{\pi D^2}{4} \text{ etc} \end{aligned}$$

Bending

$$\begin{aligned} \frac{\sigma}{y} &= \frac{M}{I} = \frac{E}{R} \\ I &= \frac{\pi D^4}{64} \text{ or } \frac{BD^3}{12} \end{aligned}$$

Torsion

$$\begin{aligned} \frac{\tau}{r} &= \frac{T}{J} = \frac{G\theta}{L} \\ J &= \frac{\pi D^4}{32} \text{ etc} \end{aligned}$$

$E$  = Young's modulus:  $\sigma$ =stress:  $\epsilon$ =strain

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### Conversion Factors

Time: 1 h = 60 min = 3600 s	Temperature difference: 1C = 1.8°F
Volume: 1m <sup>3</sup> = 10 <sup>3</sup> dm <sup>3</sup> = 10 <sup>3</sup> litre = 36.31ft <sup>3</sup> = 220 UKgal	
Energy: 1 kJ = 10 <sup>3</sup> Nm	Force: 1 N = 0.2248 lbf
Pressure: 1 bar = 10 <sup>5</sup> Pa (Nm <sup>-2</sup> ) = 14.50 lbf in <sup>-2</sup> = 750 mmHg = 10.2 mH <sub>2</sub> O	
Density 1 kg m <sup>-3</sup> = 0.062 43 lb ft <sup>-3</sup>	Mass: 1kg = $\frac{1}{0.45359237}$ lb ≈ 2.205 lb = $\frac{1}{14.5939}$ slug
1 mile = 1760 yd ≈ 1609m : 1 yd = 3 ft = 36 inches = 0.914 m : 1 m = $\frac{1}{0.3048}$ ft = 3.281 ft	
Power: 1kW = 1kJ s <sup>-1</sup> = $\frac{10^3}{9.80665 \times 75}$ metric hp ≈ 1.359 metric hp	Angle: 1 revolution = 360° = 2π

**END OF FORMULA SHEETS**

**END OF PAPER**