

UNIVERSITY OF BOLTON

SCHOOL OF ENGINEERING

**MSC SYSTEMS ENGINEERING AND ENGINEERING
MANAGEMENT**

SEMESTER TWO EXAMINATION 2018/2019

ADVANCED CONTROL TECHNOLOGY

MODULE NO: EEM7015

Date: Monday 20th May 2019

Time: 10:00 – 12:00

INSTRUCTIONS TO CANDIDATES:

There are TWO sections

Section A - You must answer either Q1a
OR Q1b from Section A

Section B - ANY TWO questions from
Section B

All questions carry equal marks.

Marks for parts of questions are shown in
brackets.

All working must be shown. A numerical
solution to a question obtained by
programming an electronic calculator will
not be accepted.

SECTION A – YOU MUST ANSWER Q1(a) OR Q1(b).
PLEASE DO NOT ANSWER BOTH

Q1.

(a) For the circuit shown in Fig.1 below:

- i) From Kirchoff's current law write down the second order differential equation that describes the relationship between inductor current and the current source. **(8 marks)**
- ii) Construct the state space equations and find the A, B, C and D matrices, where A, B, C, and D have their usual meaning **(12 marks)**
- iii) If $R=X_L=X_C=30$ ohms for 50 Hz frequency, find the system transfer function and determine its stability from the examination of system characteristic equation. **(5 marks)**
- iv) Determine the discrete-time state-space matrices A_d, B_d . **(8 marks)**

Total 33 marks

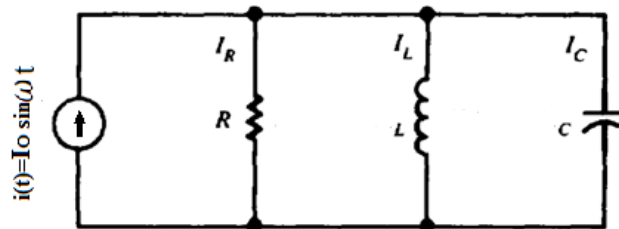


Fig.1 Parallel RLC circuit

(b) From the mass-spring-damping system of Fig. 2 shown below:

- i) Write down the second order differential equation that describes the relationship between the displacement Y and the applied force F .

(8 marks)

- ii) Construct the state space equations and find the A, B, C and D matrices, where A, B, C, and D have their usual meaning and

$$K=1 \text{ N/m}, C=2 \text{ N/(m/s)}, M=10 \text{ N/(m/s}^2\text{)}$$

(12 marks)

Question 1 continues over the page....

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Question 1 continued....

- iii) Find the system transfer function and determine its stability from the examination of system characteristic equation. **(5 marks)**

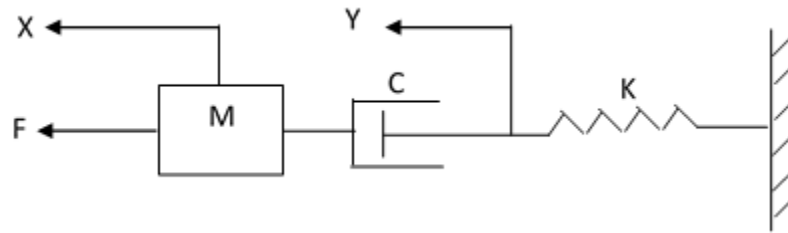


Fig.2 a mass-spring-damping system

- iv) Determine the discrete-time state-space matrices A_d , B_d . **(8 marks)**

Total 33 marks

END OF SECTION A

PLEASE TURN THE PAGE FOR SECTION B.....

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SECTION B – ANSWER ANY TWO QUESTIONS

Q2. A specific plant is given by

$$\dot{x} = A \cdot x + B \cdot u$$

$$\text{Where } A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -5 & -6 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

The system uses the state feedback control $u = -Kx$.

i) Is the system controllable? **(10 marks)**

ii) Design the regulator system shown in Fig.3 below if the desired closed-loop poles are:

$$s = -3 \mp j2, \quad s = -12$$

(15 marks)

iii) Find the new transfer function of the regulated plant and prove its stability using the factorization of its characteristic equation. **(8 marks)**

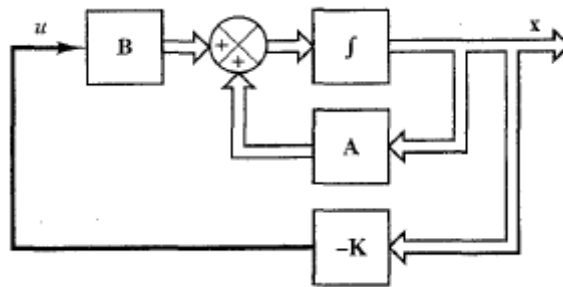


Fig.3 Regulator system

Total 33 marks

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Q3 (a) Explain the procedures of a fuzzification, a rule based evaluation, and a defuzzification. You may use examples to help and support your explanations **(9 marks)**

(b) Consider three fuzzy subsets of the set X ,
 $X = \{a, b, c, d, e, f, g\} = \{0, 1, 2, 3, 4, 5, 6\}$
 referred to as A_1 , A_2 and A_3

$$A_1 = \{0.3/a, 0.4/b, 0.7/c, 0.9/d, 1.0/e, 0.3/f, 0/g\}$$

$$A_2 = \{0.1/a, 1.0/b, 0.8/c, 0.6/d, 0.5/e, 0.3/f, 0.2/g\} \text{ and}$$

$$A_3 = \{0.8/a, 0.8/b, 0.6/c, 0.4/d, 0.3/e, 0.2/f, 0.1/g\}$$

Conduct the following Fuzzy Set Operations:

(i) The **support** of A_1 , A_2 and A_3 **(2 marks)**

(ii) The **core** of A_1 , A_2 and A_3 **(2 marks)**

(iii) The **cardinality** of A_1 and A_2 **(2 marks)**

(iv) The **complement** of A_2 and A_3 **(2 marks)**

(v) The **union** of A_1 , A_2 and A_3 **(1 mark)**

(vi) The **intersection** of A_1 , A_2 and A_3 **(1 mark)**

(vii) The new set B , if $B = A_1^2$ **(1 mark)**

(viii) The new set C , if $C = 0.7A_2$ **(1 mark)**

(ix) The new set D , for an alpha cut at $A_{30.7}$ **(1 mark)**

(x) Defuzzification of the set A_1 by using the central of gravity (COG) technique. **(2 marks)**

(xi) Defuzzification of the set A_3 by using the Sugeno method. **(1 mark)**

(c) Compare and contrast Mamdani's fuzzy inference technique with the Sugeno's inference method. **(8 marks)**

Total 33 marks

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- Q4** (a) Explain what frequency response is and briefly describe the merits for using frequency response to aid the design and analysis of systems. **(8 marks)**
- (b) Figure Q4(b) on page 6 presents a closed loop control system with Bode plots.
- (i) Identify the controller, plant and controlled plant on the plot. **(3 marks)**
 - (ii) Distinguish the type of the controller used and provide an equation for the controller. **(8 marks)**
 - (iii) Explain whether the controller has been optimised or not. **(5 marks)**
 - (iv) Design an improved controller on the Bode plot, to improve the performances of the system. **(9 marks)**

Question 4 continues over the page...

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Question 4 continued....

You can write your answers in the Bode diagram attached. Please make sure that you have written down your ID number on the sheet.

Student ID: _____

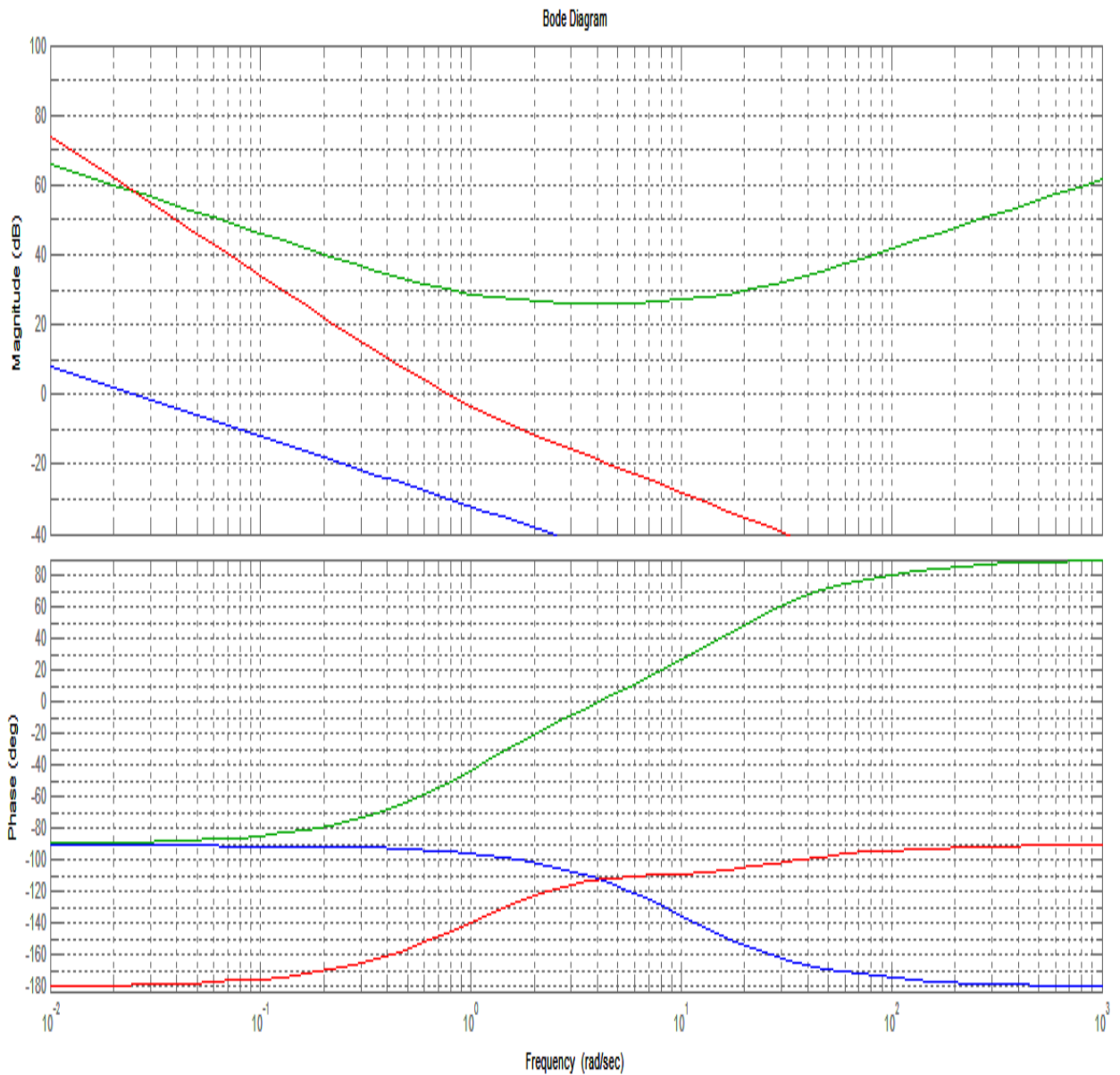


Figure Q4(b) Bode Diagrams

Total 33 marks

END OF QUESTIONS