

UNIVERSITY OF BOLTON

WESTERN INTERNATIONAL COLLEGE FZE

BENG (HONS) CIVIL ENGINEERING

SEMESTER TWO EXAMINATION 2018/2019

MATHEMATICS AND STRUCTURAL DESIGN

MODULE NO: CIE4012

Date: Wednesday 29th May 2019

Time: 10.00am - 1.00pm

INSTRUCTIONS TO CANDIDATES: There are FIVE questions on this paper.

Answer ALL questions.

Answer Section A and Section B questions in separate answer books.

Marks for parts of questions are shown in the brackets.

This examination paper carries a total of 100 marks.

Formula sheet for Section B is attached on Page 6 of this paper.

The necessary design aid data for and formula sheet for Section A will be provided at the examination hall.

All working must be shown. A numerical solution to a question obtained by programming an electronic calculator will not be accepted.

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Mathematics and Structural Design
Module No. CIE4012

SECTION A: STRUCTURAL DESIGN

Question 1: Steel Beam Design (General Aid for Design provided on Page 3)

Figure 1 shows a plan view of the first floor of an office building. The office building has a ground floor and first floor with identical layouts. For the steel beam **CD** along the **grid line 3**,

- Prepare a set of manual design calculations to choose a beam size of minimum weight and most economical. (9 marks)
- Sketch the cross-section of the chosen steel beam section (5 marks)
- Show the suitability of the chosen beam for bending, compression, shear strength, web shear buckling and combined bending and shear check. (13 marks)
- Assume beam **CD** to be simply supported and calculate the vertical deflection at mid-span of the beam **CD** to check whether it is satisfactory. (3 marks)

Total 30 marks

Question 2: Steel Column Design (General Aid for Design provided on Page 3)

For the plan view shown in **Figure 1** provided on **page 3**, Prepare a set of manual design calculations for the steel column **D** along the **grid line 2** at the ground floor if the floor to floor height is 3.2m.

- Calculate the load acting on Column D. Ignore the self-weight of columns. (10 marks)
- Choose a suitable steel section for the column D which must be economical. (4 marks)
- Design the column for buckling and compression resistance (6marks)

Total 20 marks

Please turn the page for Figure 1 and the General Aid for Design

Please turn the page

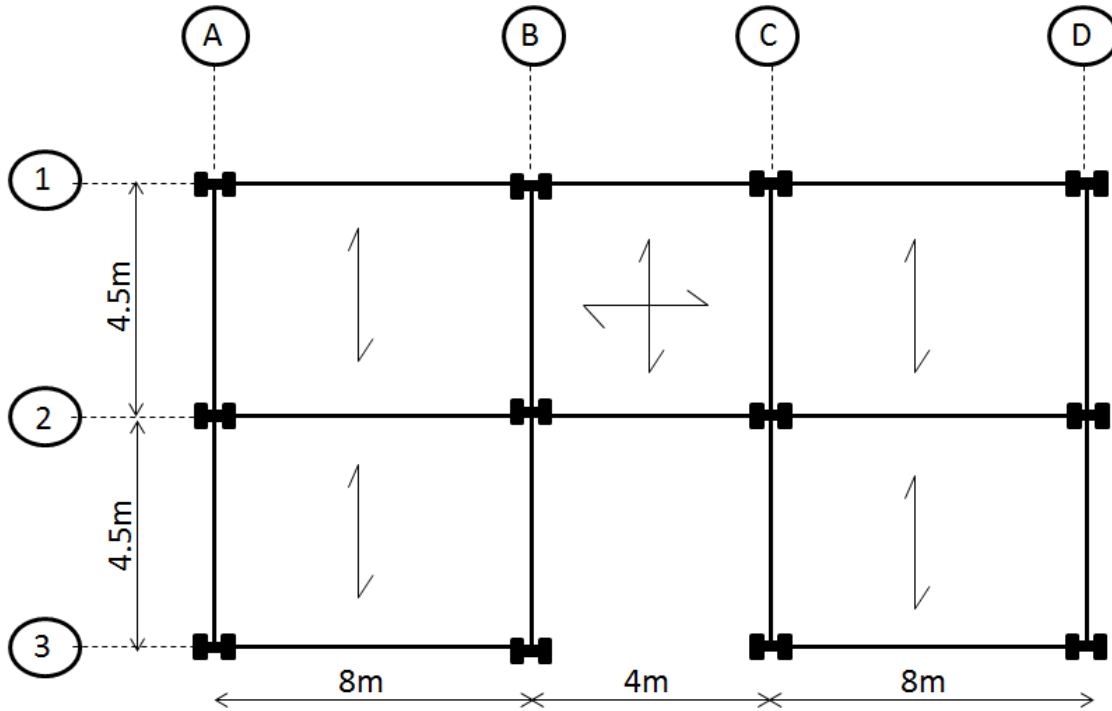


Figure 1: Plan of the first floor of an office building

General Aid for Design

- i. The thickness of each slab is 200mm (with a unit weight of 25 kN/m^3) with 50mm thick screed (with a unit weight of 24 kN/m^3) over it
- ii. The slabs are subjected to a live load of 6.0 kN/m^2 each
- iii. Consider the loadings on the slabs to be the same on each floor
- iv. The self-weight of the steel beams are 1.5 kN/m each
- v. Assume the column is carrying axial force only and pinned at both ends.
- vi. The Young's modulus of steel should be taken as 210000 N/mm^2
- vii. Steel grade of S275 is considered for the whole structure
- viii. Suggested limit for vertical deflection in steel beams here is $L/200$

END OF SECTION A

Please turn the page for SECTION B

SECTION B: MATHEMATICS

Question 3

Using suitable integration techniques, determine the following indefinite integrals, simplifying all the solutions.

a. $y = \int \frac{9}{(x-1)(x+2)^2} dx$ (8 marks)

b. $y = \int e^{5x} \sin 3x dx$ (6 marks)

c. $y = \int x^2 \sin x dx$ (6 marks)

d. $y = \int \frac{(x^2-1)(x-1)}{x(x-1)} dx$ (5 marks)

Total 25 marks

Question 4

- a. The bending moment 'M' of a beam is given by

$$\frac{dM}{dx} = -w(l-x)$$

Where 'w' the uniformly distributed load in kN/m of the beam, 'x' is the distance of the support from a section X-X as shown in Figure 4.a. Determine

'M' in terms of 'x' if $M = \frac{1}{2}wl^2$ when 'x'=0.

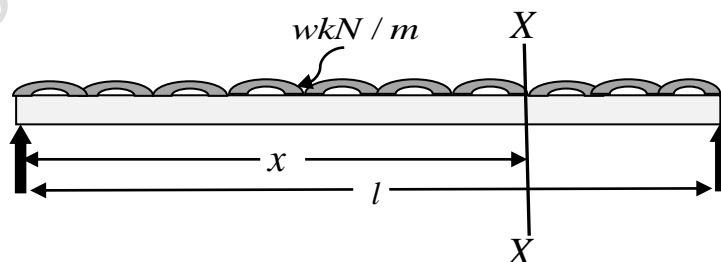


Figure 4.a- Simply Supported beam carrying UDL

(5 marks)

Question 4 continued over the page

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b. A differential equation relating the difference in tension 'T', pulley contact angle ' θ ' and coefficient of friction ' μ ' is given as $\frac{dT}{d\theta} = \mu T$. Coefficient of friction is given as $\mu = 0.30$. Slipping starts when $\theta = 0$ and $T = 150\text{N}$.

i. Determine the tension at the point of slipping when $\theta = 2\text{radians}$

ii. Determine the value of θ when T is 300N

(7 marks)

c. Find the partial derivatives of $f(x, y, z) = xyz^2 + 3xy - z$ with respect to x, y and z

(6 marks)

d. Sketch the curves $y = x^2 + 3$ and $y = 7 - 3x$ and determine the area enclosed by them.

(7 marks)

Total 25 marks

END OF SECTION B

END OF QUESTIONS

Formula sheet over the page

Please Turn the Page

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Formula Sheet

f(x)	$\int f(x) dx$ all '+c'
2x	x^2
x	$\frac{1}{2} x^2$
k (constant)	$k x$
x^n	$\frac{1}{n+1} x^{n+1}$
$\frac{1}{x}$	$\ln x$
e^x	e^x
e^{kx}	$\frac{e^{kx}}{k}$
$\sin x$	$-\cos x$
$\cos x$	$\sin x$
$\sin kx$	$-\frac{\cos kx}{k}$
$\cos kx$	$\frac{\sin kx}{k}$

END OF PAPER