[ENG17]

UNIVERSITY OF BOLTON

SCHOOL OF ENGINEERING

BENG (HONS) ELECTRICAL & ELECTRONIC ENGINEERING

SEMESTER ONE EXAMINATION 2018/2019

INTERMEDIATE ELECTRICAL PRINCIPLES & ENABLING POWER ELECTRONICS

MODULE NO: EEE5013

Date: Monday 14th January 2019

Time: 10:00 – 12:30

INSTRUCTIONS TO CANDIDATES:

There are <u>SIX</u> questions.

Answer <u>ANY FOUR</u> questions.

All questions carry equal marks.

Marks for parts of questions are shown in brackets.

Electronic calculators may be used provided that data and program storage memory is cleared prior to the examination.

CANDIDATES REQUIRE:

Formula Sheet (attached).

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Q1.

(a) Determine the input voltage (V_{in1}) from a cascaded operational amplifier circuit as shown in Fig.Q1(a).



Fig.Q1 (a): A cascaded operational amplifier circuit.

[5 marks]

(b)



Fig.Q1 (b) An Operational amplifier integrator Circuit

A summing inverting negative feedback operation circuit, as shown in Fig. Q1 (b) with V_{in} , resistors R_{in} and capacitor C, and an output of V_{out} .

Derive the formula for the output of the circuit in Fig.Q1(b) in term of R_{in} , C and V_{in} .

[10 marks]

ii) If a 0 to -1 volts repetitive input signal is applied to the integrator circuit, draw the output signal over time for four period time cycle.

[5 marks]

Question 1 continues over the page.... PLEASE TURN THE PAGE....

Question 1 continued....

(c) Fig.Q1(c) shows the voltage gain against the frequency of an op-amp. Determine the cutoff frequency of an op-amp having a unit gain frequency $f_1 = 50$ MHz and voltage differential gain $G_d = 25 V/\mu V$.



Fig.Q1 (c) An Operational amplifier's gain verse frequency

[5 marks]

Total 25 marks

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Q2.

(a) A half-wave rectifier circuit is composed from an AC source with RMS voltage of 120 V and a frequency of 60 Hz, a diode, an inductor of 10 mH, and a load resistor of 5 ohms. Calculate and plot the current i along with v_s .

[15 marks]

- (b) A single-phase full-bridge inverter is operated from a 48 V battery and is supplying power to a pure resistive load of 10 ohms. Determine:
- i) The fundamental output voltage and the first five harmonics. [5 marks]
- ii) Output RMS power and output fundamental power

[2 marks] [3 marks]

iii) Transistor switch ratings

Total 25 marks

Q3.

(a) A simple DC chopper is operating at a frequency of 2 kHz from a 96 V DC source to supply a load resistance of 8 ohms. The load time constant is 6 millisecond. if the average load voltage is 57.6 V, find:

i)	Ton period of the chopper	[3 marks]
ii)	The average load current	[4 marks]
iii)	The magnitude of the ripple current and its RMS value	[8 marks]

- (b) Prove that :
- i) the line-to-line voltage of a balanced 3-phase voltages leads its corresponding phase voltage by 30° [5 marks]
- ii) the line-to-line current of a balanced 3-phase currents lags its corresponding phase current by 30°. [5 marks]

(Hint: You may use the circuit and phasor diagrams to support your mathematical derivations for both branches i and ii.)

Total 25 marks

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Q4.

(a) Explain the power factor correction of a constant voltage inductive load. What is its importance in relation to reactive power utilisation and the supply current ? You may use a circuit diagram and the power triangle to answer this question.

[9 Marks]

(b) For the circuit shown in Fig. Q4(b).

i) Calculate the voltage at node A and node B. You may use KCL in your answer.

[10 marks]

ii) Draw the voltage and current phasor diagrams. Take V_B as a reference phasor.

[6 marks]



Total 25 marks

Q5.

(a) A MOSFET Device (MTP14N06A) has load current of 5 A (rms), find its respective junction temperature at steady state. Given that $R_{\theta ca} = 5 \text{ °C/W}$, $R_{DS (on)} = 0.2 \Omega$, $R_{\theta jc} = 4.3 \text{ °C/W}$ and $P_{D(max)} = 70 \text{ W}$.

(8 marks)

(b) An MOSFET IRF440 is required to operate at 30% duty cycle at the switching frequency of 10 kHz. Given the max. junction temperature $T_{j(max)}$ = 80 °C, and the case temperature $T_{c(case)}$ =40°C with ambient temperature $T_{A(ambient)}$ =30°C, Rcs= 0.02 °C/W, find

(i) The transient impedance Z

(ii) The Peak Power and the maximum current

(iii) The required heat sink

(5 marks)

(6 marks)

(6 marks)

Total 25 marks

Q6.

(a) Enumerate the basic grounding system then explain what is meant by equipment grounding. (10 marks)

(b) A rectangular plank floats in water. The base of the plank has a width of 25 cm, and a length of 120 cm. The thickness of the plank is 4 cm, of which a uniform 3.0 cm is below water level.

i) Calculate the pressure at the bottom of the plank, and thus the total upwards force from the water. (4 marks)

ii)	What is the weight of the plank, and what is its mass?	(4 marks)
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- iii) What is the density of the plank?
- iv) If the plank later reaches sea-water, which has a density of 1027kg/m³, how much <u>higher</u> will it float in the sea water? (5 marks)

Total 25 marks

(2 marks)

END OF QUESTIONS

Formula sheets over the page....

Formula sheet

These equations are given to save short-term memorisation of details of derived equations and are given without any explanation or definition of symbols; the student is expected to know the meanings and usage.

Converters:

$$\% \text{THD}_{i} = 100 \times \frac{I_{\text{dis}}}{I_{s1}}$$
$$= 100 \times \frac{\sqrt{I_{s}^{2} - I_{s1}^{2}}}{I_{s1}}$$
$$= 100 \times \sqrt{\sum_{h \neq 1} \left(\frac{I_{sh}}{I_{s1}}\right)^{2}}$$

$$PF = \frac{V_s I_{s1} \cos \phi_1}{V_s I_s} = \frac{I_{s1}}{I_s} \cos \phi_1$$

 $DPF = \cos \phi_1$

 $PF = \frac{I_{s1}}{I_s} DPF$

$$PF = \frac{1}{\sqrt{1 + THD_i^2}} DPF$$

 $A_u = \sqrt{2}V_s(1 - \cos u) = \omega L_s I_d$

$$\cos u = 1 - \frac{\omega L_s I_d}{\sqrt{2} V_s}$$

$$V_d = 0.45V_s - \frac{\operatorname{area} A_u}{2\pi} = 0.45V_s - \frac{\omega L_s}{2\pi} I_d$$
$$V_d = 1.35 V_{LL} \cos\alpha - 3 \frac{\omega L_s}{\pi} I_d$$

 $\cos(\alpha + u) = \cos \alpha - 2 \frac{\omega L_s}{\sqrt{2} V_{LL}} I_d$

$$\gamma = 180 - (\alpha + u)$$

$$V_{L} = \left[\frac{1}{T} \int_{0}^{T} v_{L}^{2}(t) dt\right]^{1/2}$$

$$V_{dc} = \frac{1}{T} \int_{0}^{T} v_{L}(t) dt$$

$$TUF = \frac{P_{dc}}{V_{s}I_{s}} = \frac{V_{dc}I_{dc}}{V_{s}I_{s}}$$

$$RF = \frac{V_{ac}}{V_{dc}}$$

$$\sigma = \frac{P_{dc}}{P_{L}} = \frac{V_{dc}T_{dc}}{V_{L}I_{L}}$$

$$FF = \frac{V_{L}}{V_{dc}} \quad \text{or} \quad \frac{I_{L}}{I_{dc}}$$

$$V_{d\alpha} = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_{max} \sin(\omega t) d(\omega t) = \frac{V_{max}}{2\pi} \left(1 + \cos\alpha\right)$$

$$\begin{split} V_{ph} &= \frac{v}{\sqrt{3}} \ , I_{ph} = I \ for \ star \ connection, \ V_{ph} = V, \ I_{ph} = \frac{I}{\sqrt{3}} \ for \ delta \ connection \\ S &= \sqrt{3}VI \ V.A, \ P = \sqrt{3}VIcos\theta \ W., \\ Q &= \sqrt{3}VIsin\theta \ V.A.r \\ Q_{c} &= \sqrt{3}VI_{c} \ V.A.r, \ X_{c} = \frac{v}{\sqrt{3}I_{c}} \ \Omega \end{split}$$

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 $\frac{V_o}{V_{in}} = \frac{-R_f}{R_a}$

Operational amplifiers

Non-Inverting amplifier:

$$\frac{V_o}{V_i} = 1 + \frac{R_f}{R_a}$$

Inverting amplifier:

$$V_o = -R_f \left(\frac{V_a}{R_a} + \frac{V_b}{R_b} + \frac{V_c}{R_c} \right) = -R_f \sum_{j=a}^c \frac{V_j}{R_c}$$

Gain-Bandwidth Product: f1=Gdfc

$$i \xrightarrow{v_c} v_c = \frac{1}{C} \int i dt \quad i = C \frac{dv}{dt}$$

Integrator:

$$V_o = \frac{-1}{RC} \int V_{in} \, \mathrm{dt}$$

Differentiator:

$$v_o = -RC \frac{dv_{in}}{dt}$$

Thermal analysis formula

$$\theta_{JATotal} = \theta_{JC} + \theta_{CA} = \frac{T_J - T_A}{P}$$

$$\theta_{JATotal} = \theta_{JC} + \theta_{CS} + \theta_{SA} = \frac{T_J - T_A}{P}$$

$$\Theta_{\rm cs} = \frac{(\rho)(t)}{A}$$

$$\boldsymbol{Z}_{\boldsymbol{\theta}\ (j-C)} = \boldsymbol{r}(\boldsymbol{t}_{p}) \times \boldsymbol{R}_{\boldsymbol{\theta}\ (j-C)}$$

$$P_{peak} = \frac{T_{j(max)} - T_{C}}{Z(t_{p}, \delta)} \text{ where } \delta = dutycycle}$$
$$P_{ave} = \delta \times P_{peak}$$

Three-phase systems



Delta to Star conversion:



$$R_{a} = \frac{R_{1}R_{2}}{R_{1} + R_{2} + R_{3}}$$
$$R_{b} = \frac{R_{2}R_{3}}{R_{1} + R_{2} + R_{3}}$$
$$R_{c} = \frac{R_{3}R_{1}}{R_{1} + R_{2} + R_{3}}$$

$$R_{1} = \frac{R_{a}R_{b} + R_{b}R_{c} + R_{c}R_{a}}{R_{b}}$$

$$R_{2} = \frac{R_{a}R_{b} + R_{b}R_{c} + R_{c}R_{a}}{R_{c}}$$

$$R_{3} = \frac{R_{a}R_{b} + R_{b}R_{c} + R_{c}R_{a}}{R_{a}}$$
PLEASE TURN THE PAGE....

Star to Delta conversion:

Gravity:

9.81 m/s $\theta_{cs} = \frac{(\rho)(t)}{\Lambda}$ Thermal resistance of the interface material: $v_0 = -R_2 C_1 \frac{dv_I}{dt}$ Output voltage of a differentiator circuit: Compressibility relationship: K = -VGeneral manometer: $\Delta P = |\Delta \rho g \Delta h|$ Venturi meter: $2\Delta P$ $v_{\rm in} = C_D$ d_{large} Force on a submerged wall: = <u>p</u>gah Drag coefficient: $\frac{F_D}{\rho v^2 A}$ C_{Drag} $\frac{1}{2}$ Flow through a small hole: $Q = C_D \sqrt{\frac{2\Delta P}{2}} A$ Flow through a rectangular slit: $Q = \frac{2}{3}C_D W\sqrt{2g} \left| (Ho + L)^{\frac{3}{2}} - Ho^{\frac{3}{2}} \right|$ PLEASE TURN THE PAGE....

Tank draining:

Flow over a rectangular weir:

Flow over a V-notch weir:

 $h^{\frac{1}{2}} = h_0^{\frac{1}{2}} - \frac{C_D a \sqrt{2g}}{2A} t$ $Q = \frac{2}{3} C_D W \sqrt{2g} H^{\frac{3}{2}}$ $Q = \frac{8}{15} C_D \tan\left(\frac{\theta}{2}\right) (2g)^{\frac{1}{2}} H^{\frac{5}{2}}$ $Q = -\frac{\pi}{128\mu} \frac{dP}{dx} D^4$ $\Delta P = \frac{2f L\rho \overline{u}^2}{D}$

Poisseuille's Law:

Darcy's Law:

Summary of phase and line voltages/currents for balanced three-phase systems.¹

Connection	Phase voltages/currents	Line voltages/currents
Y-Y	$\mathbf{V}_{an} = V_n / 0^\circ$	$\mathbf{V}_{ab} = \sqrt{3} V_p / 30^\circ$
	$V_{bn} = V_p / -120^{\circ}$	$\mathbf{V}_{bc} = \mathbf{V}_{ab} / -120^{\circ}$
	$\mathbf{V}_{cn} = V_p / + 120^\circ$	$\mathbf{V}_{ca} = \mathbf{V}_{ab}/+120^{\circ}$
	Same as line currents	$\mathbf{I}_a = \mathbf{V}_{an} / \mathbf{Z}_Y$
		$\mathbf{I}_b = \mathbf{I}_a / -120^\circ$
		$\mathbf{I}_c = \mathbf{I}_a / + 120^\circ$
$Y-\Delta$	$\mathbf{V}_{an} = V_p / 0^\circ$	$\mathbf{V}_{ab} = \mathbf{V}_{AB} = \sqrt{3} V_p / 30^\circ$
	$\mathbf{V}_{bn} = V_p / -120^{\circ}$	$\mathbf{V}_{bc} = \mathbf{V}_{BC} = \mathbf{V}_{ab} / -120^{\circ}$
	$\mathbf{V}_{cn} = V_p / +120^{\circ}$	$\mathbf{V}_{ca} = \mathbf{V}_{CA} = \mathbf{V}_{ab} / +120^{\circ}$
	$\mathbf{I}_{AB}=\mathbf{V}_{AB}/\mathbf{Z}_{\Delta}$	$\mathbf{I}_a = \mathbf{I}_{AB} \sqrt{3} / -30^\circ$
	$\mathbf{I}_{BC}=\mathbf{V}_{BC}/\mathbf{Z}_{\Delta}$	$\mathbf{I}_b = \mathbf{I}_a / -120^\circ$
	$\mathbf{I}_{CA} = \mathbf{V}_{CA}/\mathbf{Z}_{\Delta}$	$\mathbf{I}_c = \mathbf{I}_a / +120^{\circ}$
Δ - Δ	$\mathbf{V}_{ab} = V_p / \underline{0^\circ}$	Same as phase voltages
	$\mathbf{V}_{bc} = V_p / -120^{\circ}$	
	$\mathbf{V}_{ca} = V_p / +120^{\circ}$	—
	$\mathbf{I}_{AB}=\mathbf{V}_{ab}/\mathbf{Z}_{\Delta}$	$\mathbf{I}_a = \mathbf{I}_{AB} \sqrt{3/-30^\circ}$
	$\mathbf{I}_{BC} = \mathbf{V}_{bc} / \mathbf{Z}_{\Delta}$	$\mathbf{I}_b = \mathbf{I}_a / -120^\circ$
	$\mathbf{I}_{CA} = \mathbf{V}_{ca} / \mathbf{Z}_{\Delta}$	$\mathbf{I}_c = \mathbf{I}_a / +120^{\circ}$
Δ -Y	$\mathbf{V}_{ab} = V_p / 0^{\circ}$	Same as phase voltages
	$\mathbf{V}_{bc} = V_p / -120^\circ$	
	$\mathbf{V}_{ca} = V_p / +120^{\circ}$	
	Same as line currents	$\mathbf{I} = \frac{V_p / -30^\circ}{10^\circ}$
	Same as mic currents	$\mathbf{L}_a = \sqrt{3}\mathbf{Z}_Y$
		$\mathbf{I}_b = \mathbf{I}_a / -120^\circ$
		$\mathbf{I}_c = \mathbf{I}_a / +120^\circ$

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Datasheet

International **ICR** Rectifier

REPETITIVE AVALANCHE AND dv/dt RATED HEXFET[®]TRANSISTORS THRU-HOLE (TO-204AA/AE)

Product Summary

Part Number	BVDSS	RDS(on)	D
IRF440	500V	<mark>0.85Ω</mark>	8.0A

The HEXFET[®]technology is the key to International Rectifier's advanced line of power MOSFET transistors. The efficient geometry and unique processing of this latest "State of the Art" design achieves: very low on-state resistance combined with high transconductance; superior reverse energy and diode recovery dv/dt capability.

The HEXFET transistors also feature all of the well established advantages of MOSFETs such as voltage control, very fast switching, ease of paralleling and temperature stability of the electrical parameters.

They are well suited for applications such as switching power supplies, motor controls, inverters, choppers, audio amplifiers and high energy pulse circuits.



PD - 90372A

500V, N-CHANNEL



Features:

- Repetitive Avalanche Ratings
- Dynamic dv/dt Rating
- Hermetically Sealed
- Simple Drive Requirements
- Ease of Paralleling

Absolute Maximum Ratings

	-		
	Parameter		Units
ID @ VGS =0V, TC = 25°C	Continuous Drain Current	8.0	
ID @ VGS = 0V, TC = 100°C Continuous Drain Current		5.0	A
I D M	Pulsed Drain Current ①	32	
PD @ TC = 25°C	Max. Power Dissipation	125	W
	Linear Derating Factor	1.0	W/°C
VGS	Gate-to-Source Voltage	±20	V
EAS	Single Pulse Avalanche Energy ②	700	mJ
IAR Avalanche Current ①		8.0	A
EAR	Repetitive Avalanche Energy ①	-	mJ
dv/dt	Peak Diode Recovery dv/dt 3	3.5	V/ns
TJ	Operating Junction	-55 to 150	
TSTG	Storage Temperature Range		°C
	Lead Temperature	300 (0.063 in. (1.6mm) from case for 10s)	
	Weight	11.5(typical)	g

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	Parameter	Min	Тур	Мах	Units	Test Conditions
BVDSS	Drain-to-Source Breakdown Voltage	500	_	_	V	VGS = 0V, ID = 1.0mA
ΔBV _{DSS} /ΔTJ	Temperature Coefficient of Breakdown Voltage	_	0.78	_	V/°C	Reference to 25°C, ID = 1.0mA
RDS(on)	Static Drain-to-Source On-State	—	—	0.85	0	V _{GS} = 10V, I _D = 5.0A@
	Resistance	—	—	0.98	52	V _{GS} = 10V, I _D =8.0A ④
VGS(th)	Gate Threshold Voltage	2.0	—	4.0	V	$V_{DS} = V_{GS}$, $I_D = 250 \mu A$
9fs	Forward Transconductance	4.7	—	_	S (0)	V _{DS} > 15V, I _{DS} = 5.0A @
IDSS	Zero Gate Voltage Drain Current	_	—	25		V _{DS} =400V, V _{GS} =0V
		_	—	250	μA	VDS = 400V
						V _{GS} = 0V, T _J = 125°C
GSS	Gate-to-Source Leakage Forward	_	—	100	n۸	V _{GS} =20V
IGSS	Gate-to-Source Leakage Reverse	_	_	-100	IIA	VGS = -20V
Qg	Total Gate Charge	27.3	—	68.5		V _{GS} =10V, ID=8.0A
Qgs	Gate-to-Source Charge	2.0	—	12.5	nC	V _{DS} = 250V
Qgd	Gate-to-Drain ('Miller') Charge	11	—	42		
td(on)	Turn-On Delay Time	_	—	21		V _{DD} =250V, I _D =8.0A,
tr	Rise Time	_	—	73	ne	R _G =9.1Ω
^t d(off)	Turn-Off Delay Time	—	—	72	115	
tf	Fall Time	_	_	51		
L _S + L _D	Total Inductance	_	6.1	_	nH	Measured from drain lead (6mm/0.25in. from package) to source lead (6mm/0.25in. from package)
Ciss	Input Capacitance	_	1300			VGS = 0V, VDS = 25V
Coss	Output Capacitance	_	310	_	pF	f = 1.0MHz
CISS	Reverse Transfer Capacitance	_	120	_		

Electrical Characteristics @Tj = 25°C (Unless Otherwise Specified)

Source-Drain Diode Ratings and Characteristics

	Parameter		Min	Тур	Max	Units	Test Conditions
ls	Continuous Source Current (B	ody Diode)	_	_	8.0	Δ	
ISM	Pulse Source Current (Body D	iode) 1	_	_	32		
VSD	Diode Forward Voltage		_	_	1.5	V	Tj = 25°C, IS = 8.0A, VGS = 0V @
trr	Reverse Recovery Time		—	—	700	n6	Tj = 25°C, IF = 8.0A, di/dt ≤ 100A/μs
QRR	Reverse Recovery Charge		_	—	8.9	μC	V _{DD} ≤ 50V ④
ton	Forward Turn-On Time	Intrinsic tum-on time is negligible. Tum-on speed is substantially controlled by LS + LD.					

Thermal Resistance

	Parameter	Min	Тур	Max	Units	Test Conditions
RthJC	Junction to Case	_	_	1.0	*C 0.01	
RthJA	Junction to Ambient	—	—	30	C/W	Typical socket mount

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Fig. Normalized On-Resistance (RDS(on)) verse Temperature

Table. Rectangular ruse Duration verse Enective transient merma					
Rectangular Pulse Duration	Effective Transient Thermal				
(Seconds)	Impedance, Ζ _{θjc} (Ω)				
10 uS	0.08				
20 uS	0.12				
30 uS	0.18				
40 uS	0.22				
50 uS	0.30				
60 uS	0.35				

END OF PAPER